

Efficient Methods for Anomalous Pattern Detection in General Datasets

Event & Pattern Detection Lab

Carnegie Mellon University

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**Auton
Lab**

Carnegie Mellon
Heinz College
iLab: INTERDISCIPLINARY RESEARCH

**Event &
Pattern
Detection**

The logo for the Event & Pattern Detection Lab, featuring the letters 'EPD' in a stylized, overlapping font within a circular shape.

Anomalous Pattern Detection

- Two set of processes generating data
 - Typical system behavior
 - Anomalous system behavior
- Discover and characterize the anomalous processes
 - Evaluating records in isolation may be insufficient
 - Find the subsets of data that correspond to anomalous system behavior
 - An anomalous subsets is self-similar and as a group different from rest of the data



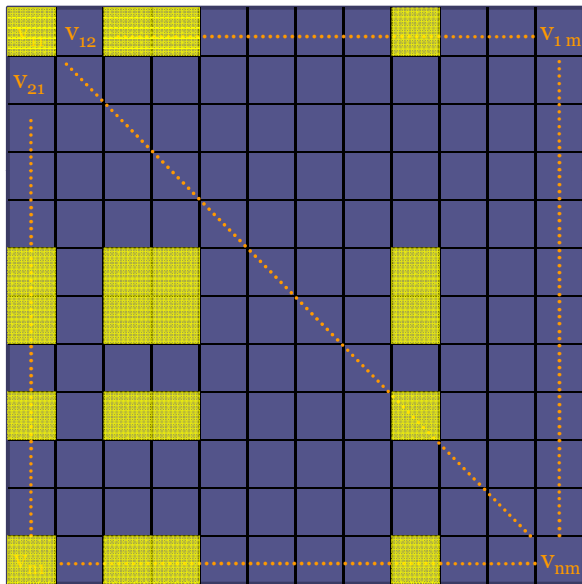
Is it Useful?

- Fraud Detection
- Network Intrusion Detection
- Anomalous Patterns of Smuggling
- Disease Surveillance
- ...And many more ways to make the world a better place

The Goal!

Attributes $A_1 \dots A_M$

Records $R_1 \dots R_N$

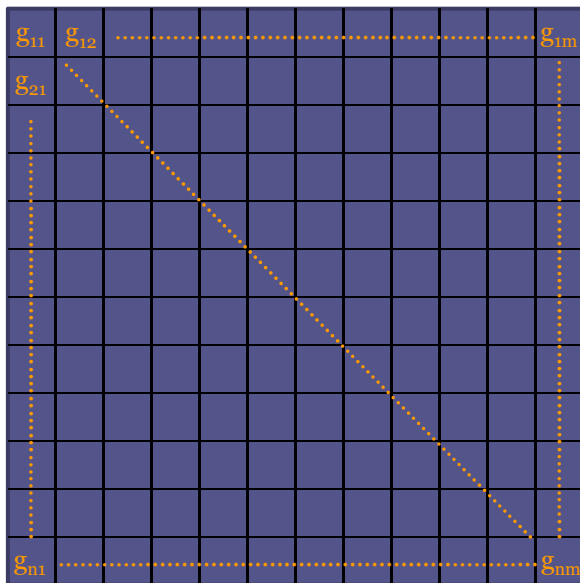


- I. Compute the anomalousness of each attribute value (for each record)
- II. Discover subsets of records and attributes that are most anomalous

Fast Generalized Subset Scan (FGSS)

Attributes $A_1 \dots A_M$

Records $R_1 \dots R_N$



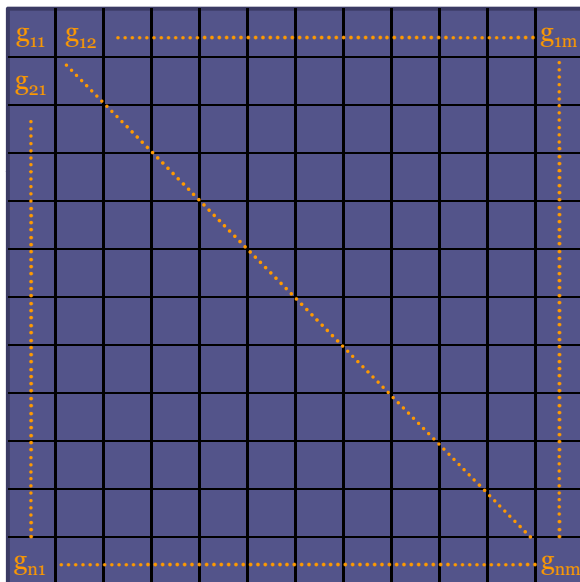
I. Compute the anomalousness of each attribute (for each record)

In order to compute the anomalousness of the data, FGSS models the data distribution under expected system behavior

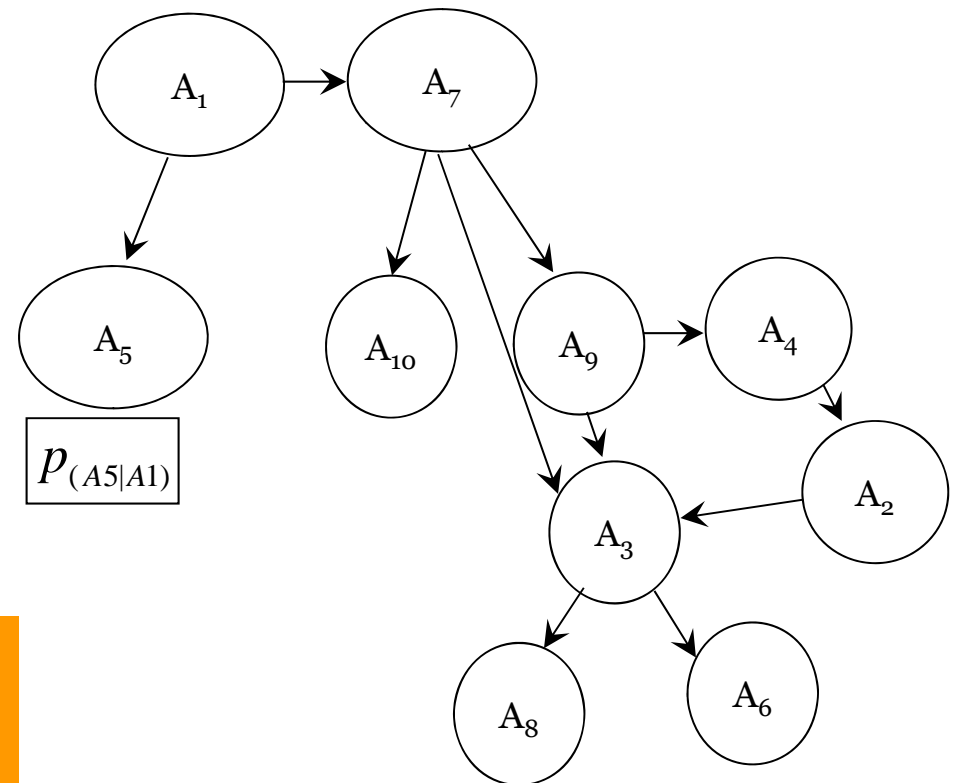
Fast Generalized Subset Scan (FGSS)

Attributes $A_1 \dots A_M$

Records $R_1 \dots R_N$



I. Compute the anomalousness of each attribute (for each record)

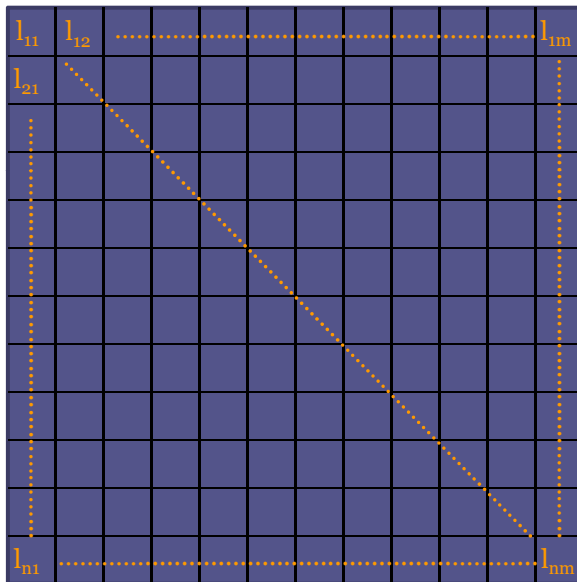


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Fast Generalized Subset Scan (FGSS)

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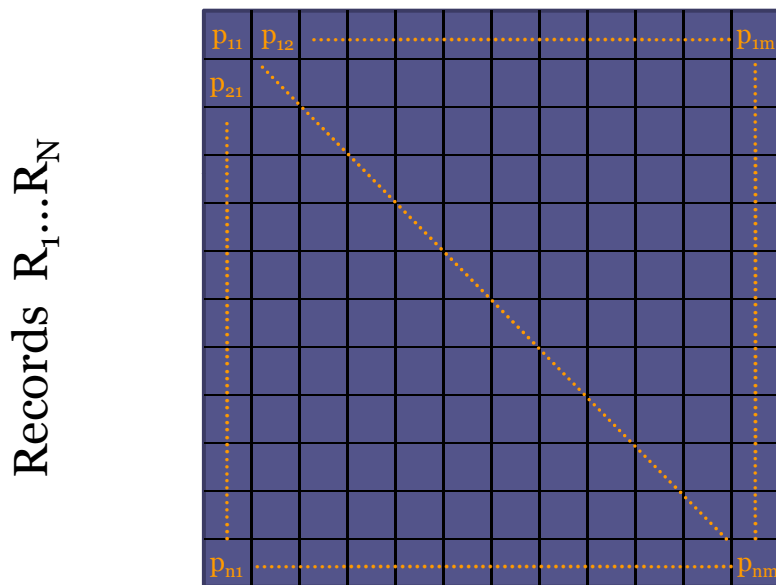


- I. Compute the anomalousness of each attribute (for each record)
 1. Learn Bayesian Network
 2. Compute attribute value likelihoods

By performing inference on the Bayesian Network, for each record we can determine the likelihood of each of its attribute values

Fast Generalized Subset Scan (FGSS)

Attributes $A_1 \dots A_M$



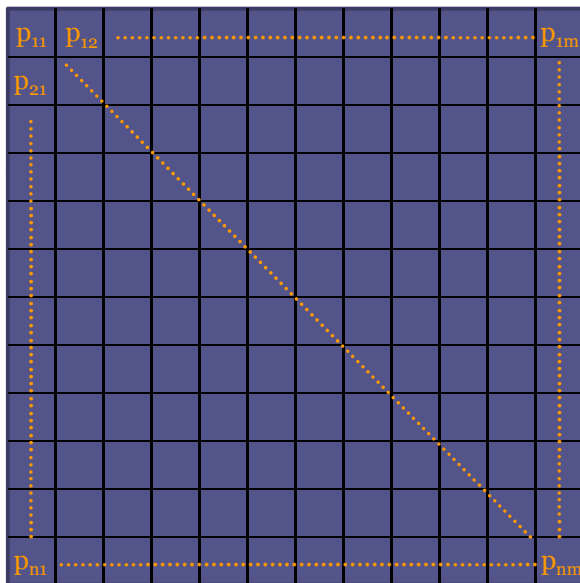
- I. Compute the anomalousness of each attribute (for each record)
 1. Learn Bayesian Network
 2. Compute attribute value likelihoods
 3. Compute empirical p-values
 - i. maps each attribute distribution to same space
 - ii. p_{ij} in $S \sim \text{Uniform}(0,1)$ under H_0

Empirical p-values are a measure, mapped onto the interval $[0,1]$, of how surprising each attribute value is given the model of normal system behavior

Fast Generalized Subset Scan (FGSS)

Attributes $A_1 \dots A_M$

Records $R_1 \dots R_N$



- I. Compute the anomalousness of each attribute (for each record)
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- II. Discover subsets of records and attributes that are most anomalous

Subsets of data with a higher than expected quantities of significantly low p-values are possibly indicative of an anomalous process

Fast Generalized Subset Scan (FGSS)

Nonparametric Scan Statistic (NPSS)

$$F(S) = \max_{\alpha} F(S) = \max_{\alpha} F_{\alpha}(N_{\alpha}, N)$$

$$N_{\alpha} = |\{p_{ij} \in S : p_{ij} \leq \alpha\}|$$

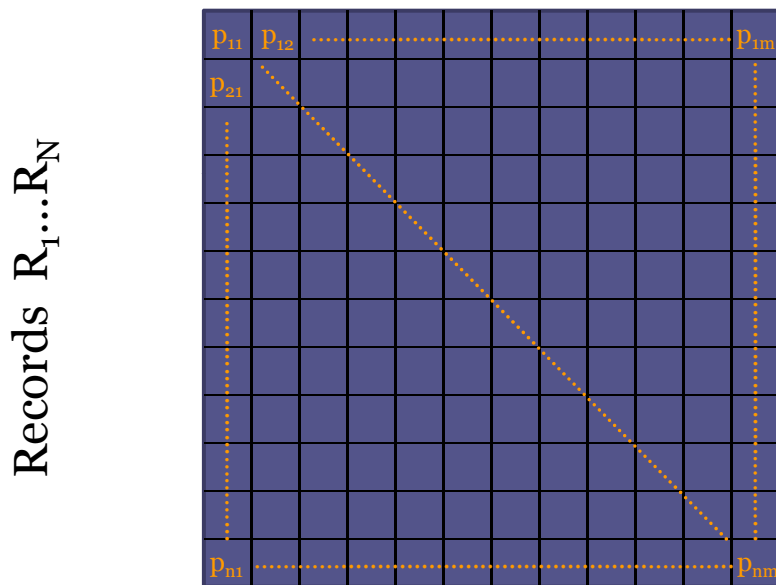
$$N_{\text{tot}} = |\{p_{ij} \in S\}|$$

- I. Compute the anomalousness of each attribute (for each record)
 1. Learn Bayesian Network
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- II. Discover subsets of records and attributes that are most anomalous
 - Evaluate subsets with NPSS

NPSS quantifies how dissimilar the distribution of empirical p-values in S are from Uniform(0,1)

Fast Generalized Subset Scan (FGSS)

Attributes $A_1 \dots A_M$



- I. Compute the anomalousness of each attribute (for each record)
 1. Learn Bayesian Network
 2. Compute attribute value likelihoods
 3. Compute empirical p-values
- II. Discover subsets of records and attributes that are most anomalous
 1. Maximize $F(S)$ over all subsets of S
 - Naïve search is infeasible $O(2^{N+M})$

Search over all possible subsets of records' p-value ranges and find the maximizing $F(S)$

Fast Generalized Subset Scan (FGSS)

Linear Time Subset Scanning Property (LTSS)

A $F(S)$ satisfies LTSS iff :

$$\max_{S \subseteq D} F(S) = \max_{i=1 \dots N} F(\{R_{(1)} \dots R_{(i)}\})$$

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We can reduce the search over records from $O(2^N)$ to $O(N \log N)$

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We only need to consider:

$$\begin{aligned} &\{R_{(1)}\} \\ &\{R_{(1)}, R_{(2)}\} \\ &\{R_{(1)}, R_{(2)}, R_{(3)}\} \\ &\vdots \\ &\{R_{(1)}, \dots, R_{(n)}\} \end{aligned}$$

We can reduce the search over records from $O(2^N)$ to $O(N \log N)$

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Fast Generalized Subset Scan (FGSS)

Linear Time Subset Scanning Property (LTSS)

A $F(S)$ satisfies LTSS iff :

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We want to maximize of subsets of records AND attributes; Observe $F(S)$ is only a function of p_{ij} , thus we can use LTSS to also maximize over the attributes

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Linear Time Subset Scanning Property (LTSS)

A $F(S)$ satisfies LTSS iff :

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We can iterate between maximizing over the records and maximizing over the attributes

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 - LTSS over records $O(N \log N)$
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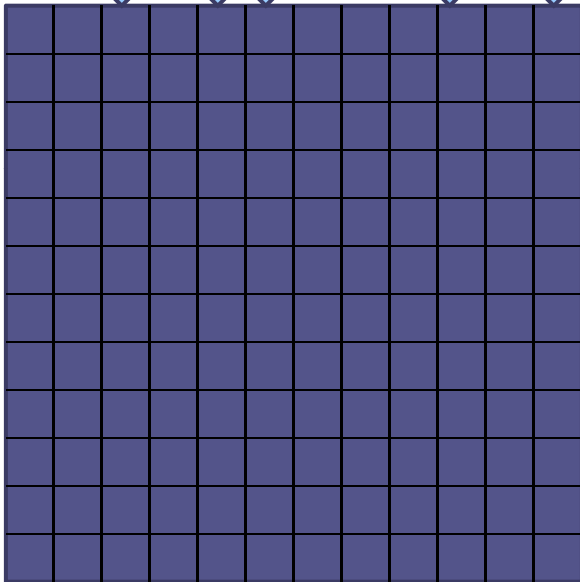
Fast Generalized Subset Scan (FGSS)

FGSS Search Procedure

Attributes $A_1 \dots A_M$



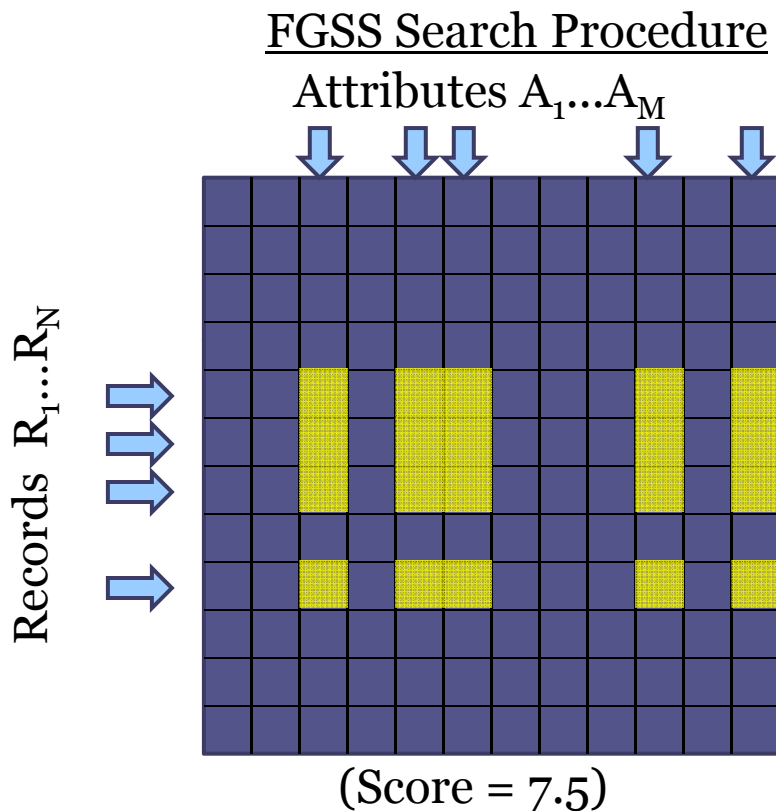
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1. Start with a randomly chosen subset of attributes

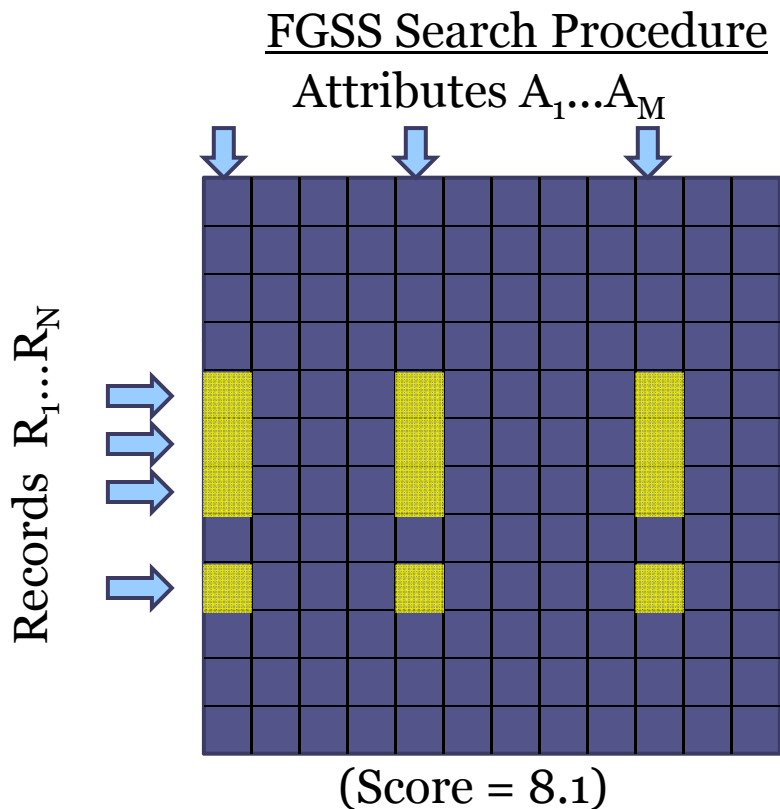
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1. Start with a randomly chosen subset of attributes
2. Use LTSS to find the highest-scoring subset of recs for the given atts

Fast Generalized Subset Scan (FGSS)

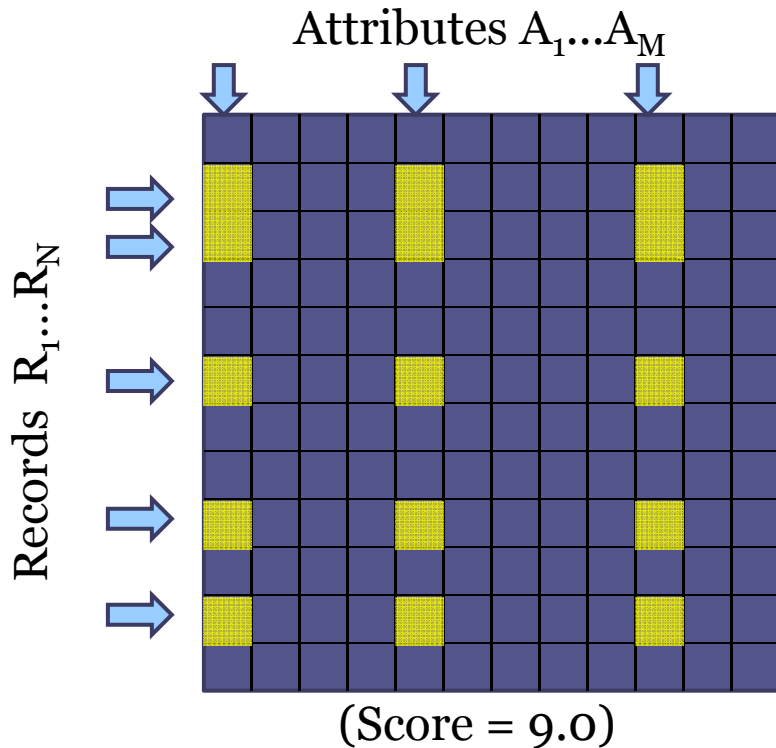


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Fast Generalized Subset Scan (FGSS)

FGSS Search Procedure

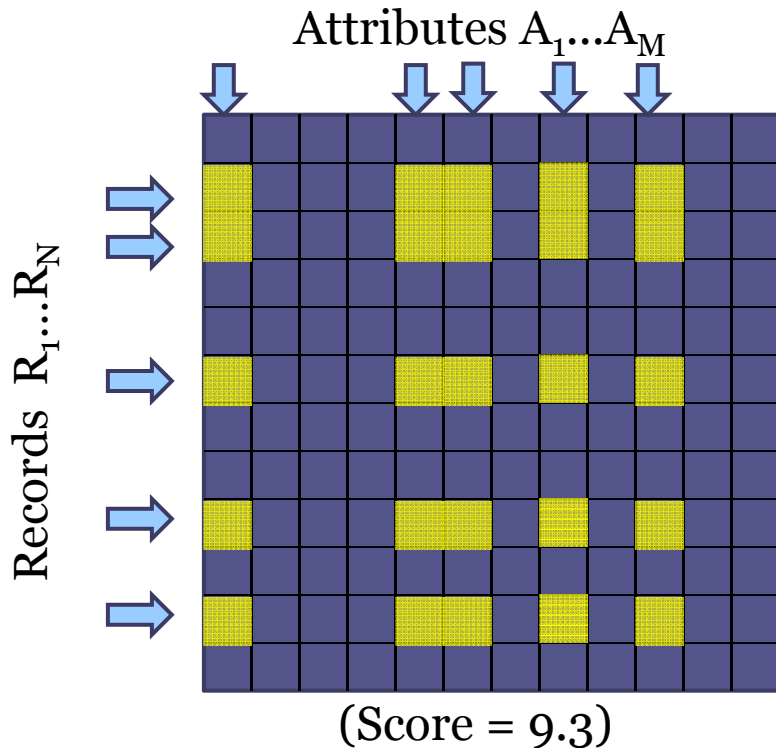


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3. Use LTSS to find the highest-scoring subset of atts for the given recs
4. Iterate steps 2-3 until convergence

Fast Generalized Subset Scan (FGSS)

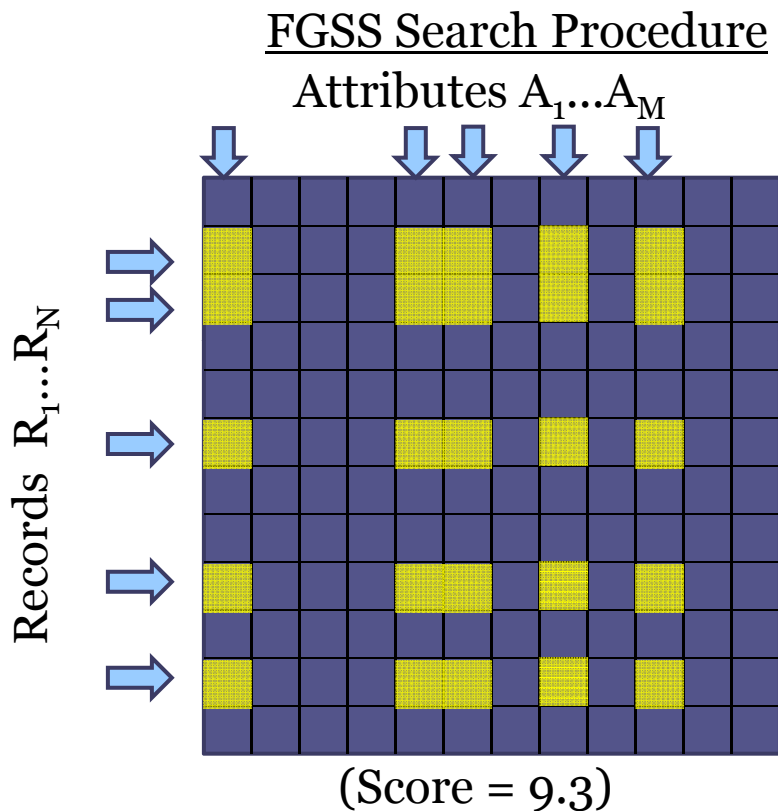
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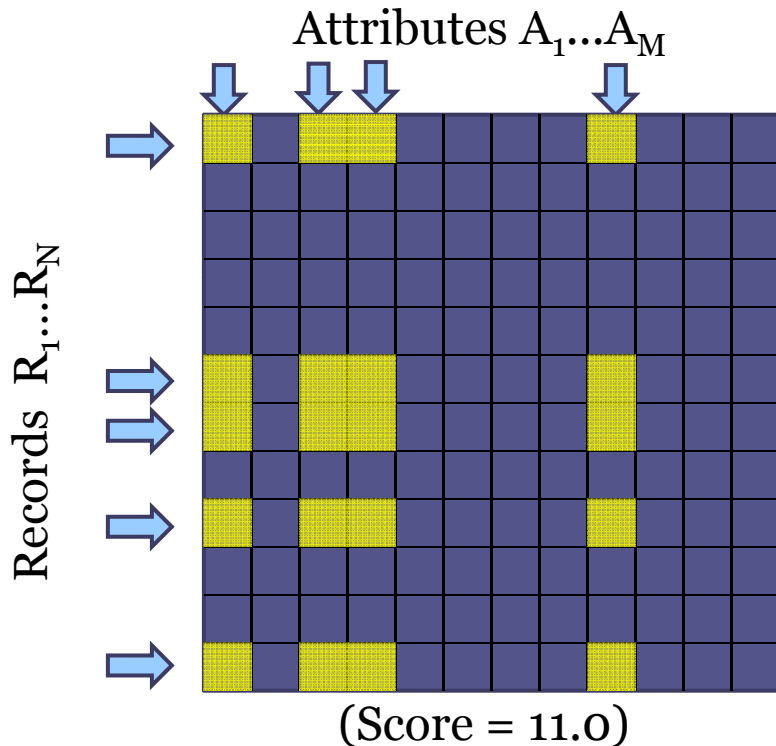
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Good News: Run time is (near) linear in number of recs & number of atts.

Bad News: Not guaranteed to find global maximum of the score function.

Fast Generalized Subset Scan (FGSS)

FGSS Search Procedure

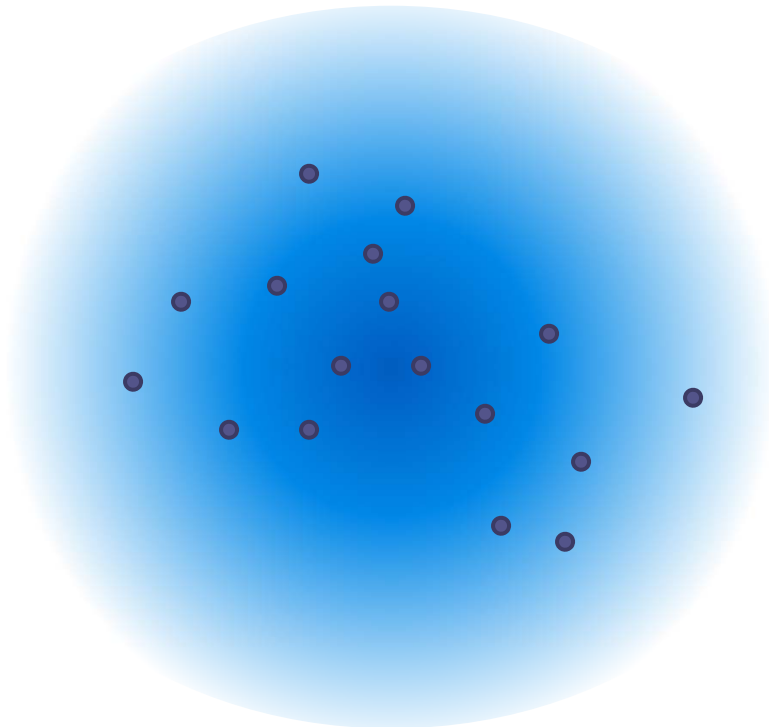


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5. Repeat steps 1-4 for 50 random restarts

Fast Generalized Subset Scan (FGSS)

FGSS Constrained Search Procedure

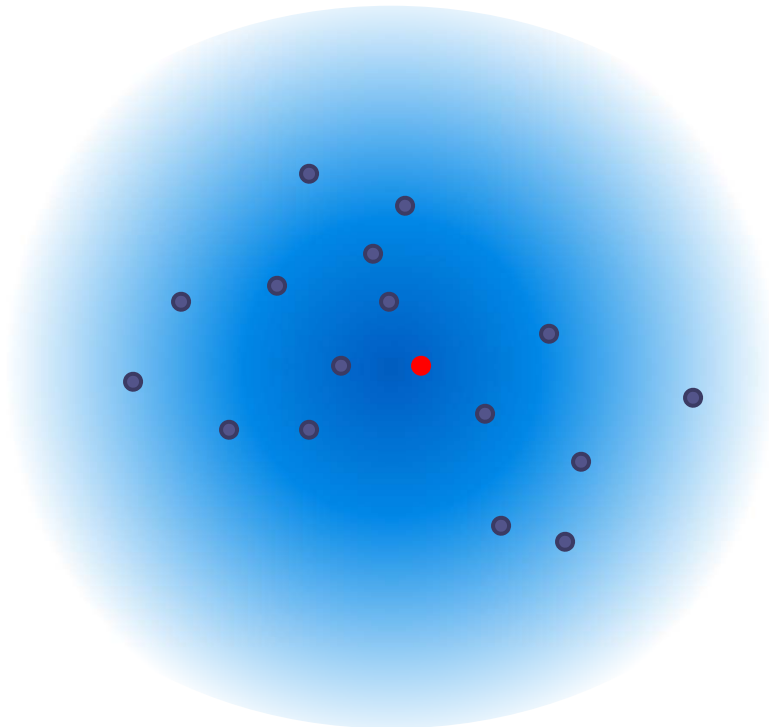


We want to enforce self-similarity, thus we create local neighborhoods.

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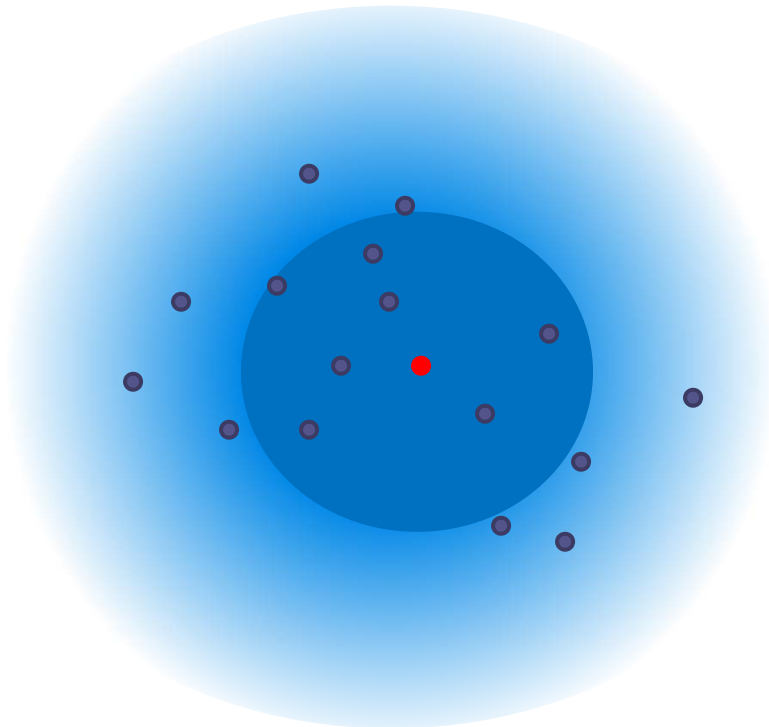


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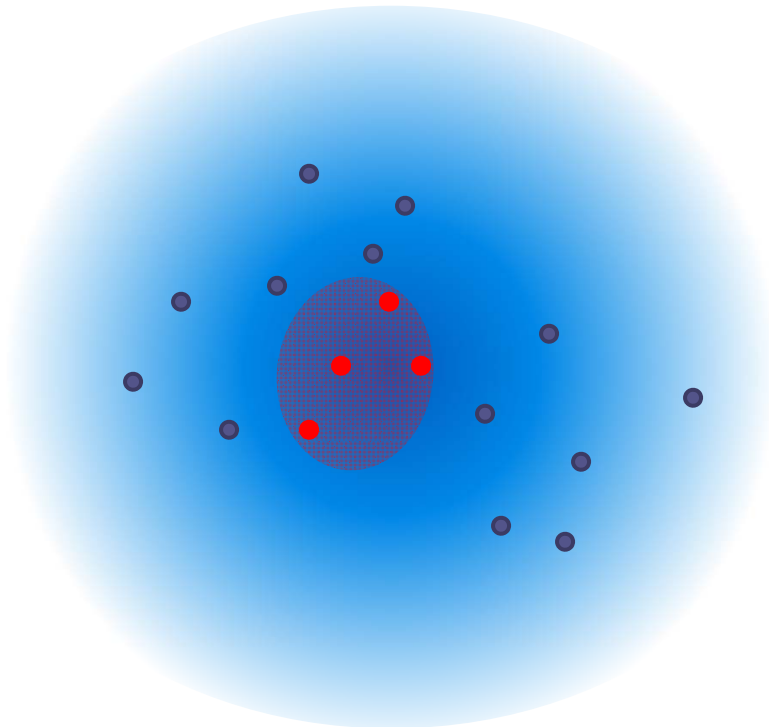


We want to enforce self-similarity, thus we create local neighborhoods defined by a center record and all other records within a max dissimilarity

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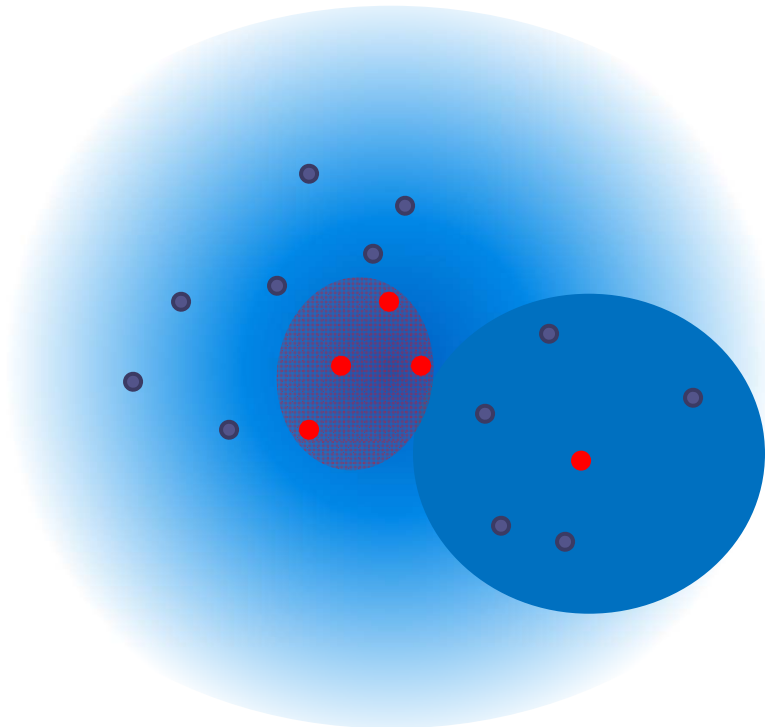


We want to enforce self-similarity, thus we create local neighborhoods, do the unconstrained search within each local neighborhood

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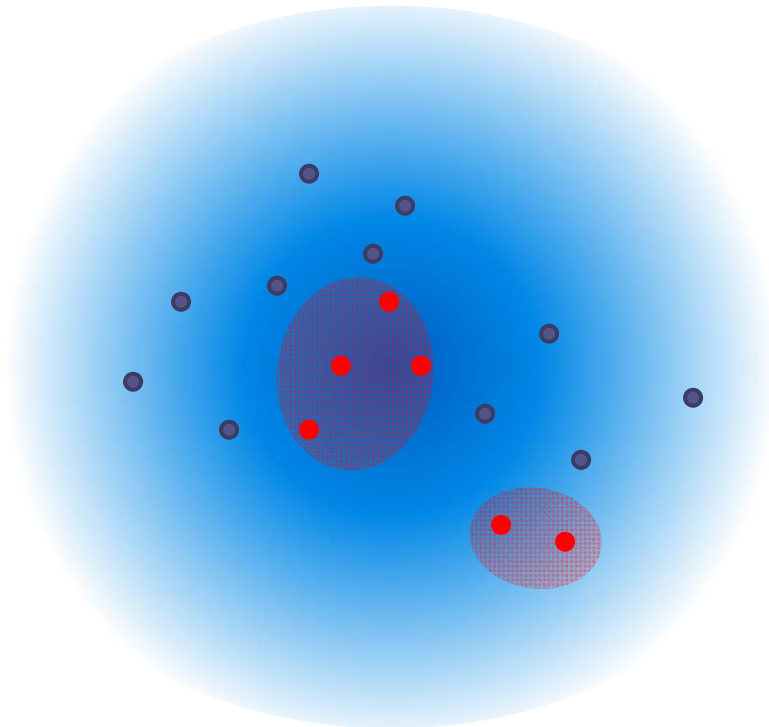


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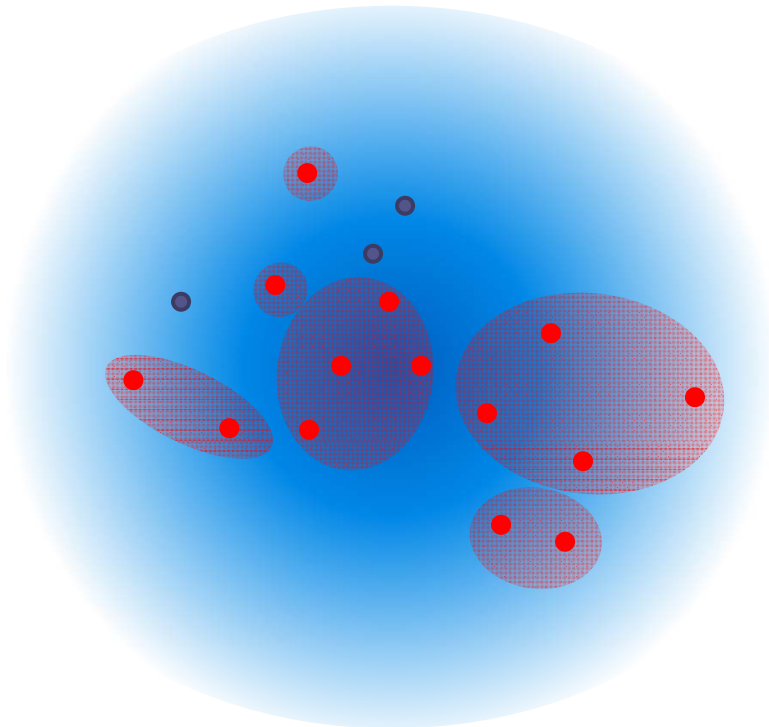


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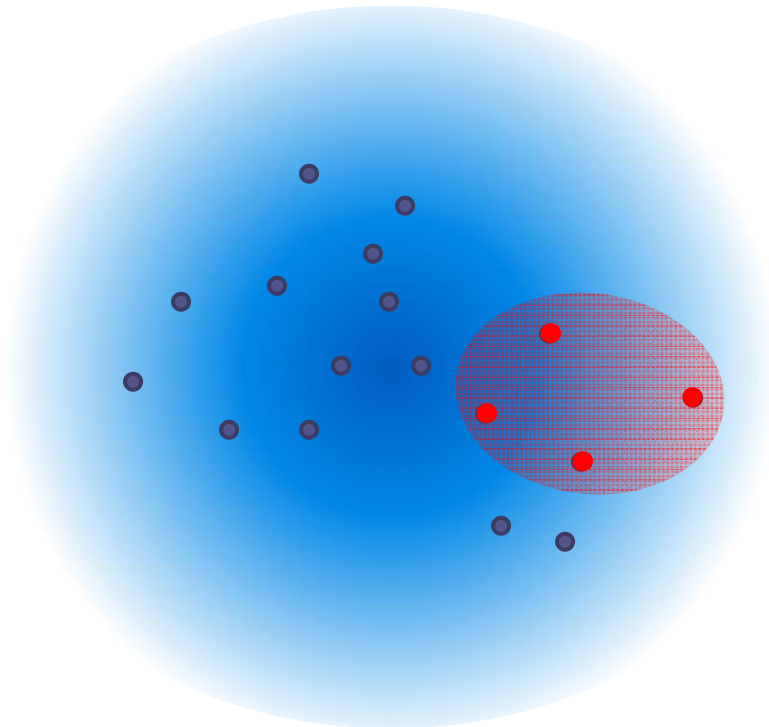


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Fast Generalized Subset Scan (FGSS)

FGSS Constrained Search Procedure



We want to enforce self-similarity, thus we create local neighborhoods, do the unconstrained search within each local neighborhood, and maximize $F(S)$ over all local neighborhoods

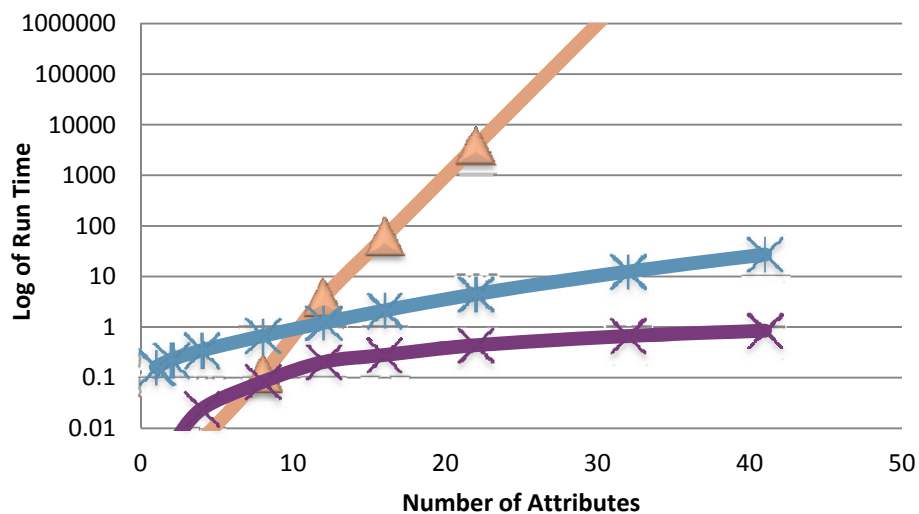
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Experiments

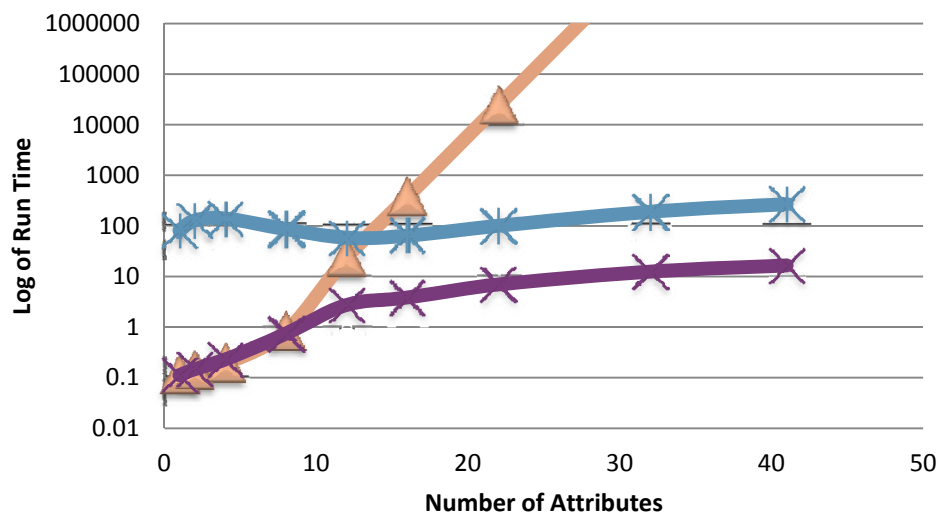
- Network Activity and Intrusion Data (KDDCUP '99)
 - 41 attributes representing extracted information from the raw data of the network connection
- BARD Simulated Anthrax Outbreak in ED visits
 - Hospital Id
 - Prodrome
 - Age Decile
 - Patient Home Zip-code
 - Chief Complaint
- U.S. Customs and Boarder Patrol Data
 - Country of origin
 - Departing & Arriving ports, Shipping line
 - Shipper's & Vessel's name
 - Commodity being shipped
- We compare FGSS to other recently proposed methods
 - Bayesian Network Anomaly Detector
 - Anomaly Pattern Detection (APD) (Das et al. 2008)
 - Anomalous Group Detection (AGD) (Das et al. 2009)

Results

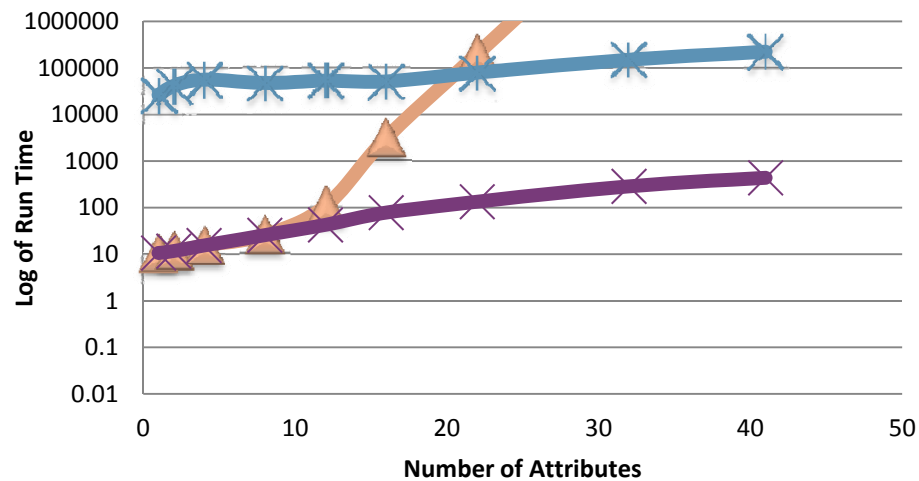
Run Times (100 Records)



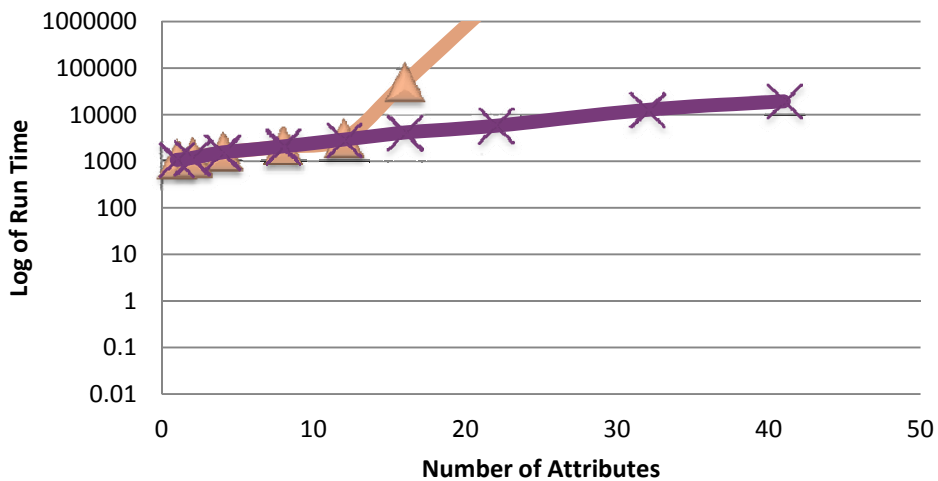
Run Times (1,000 Records)



Run Times (10,000 Records)



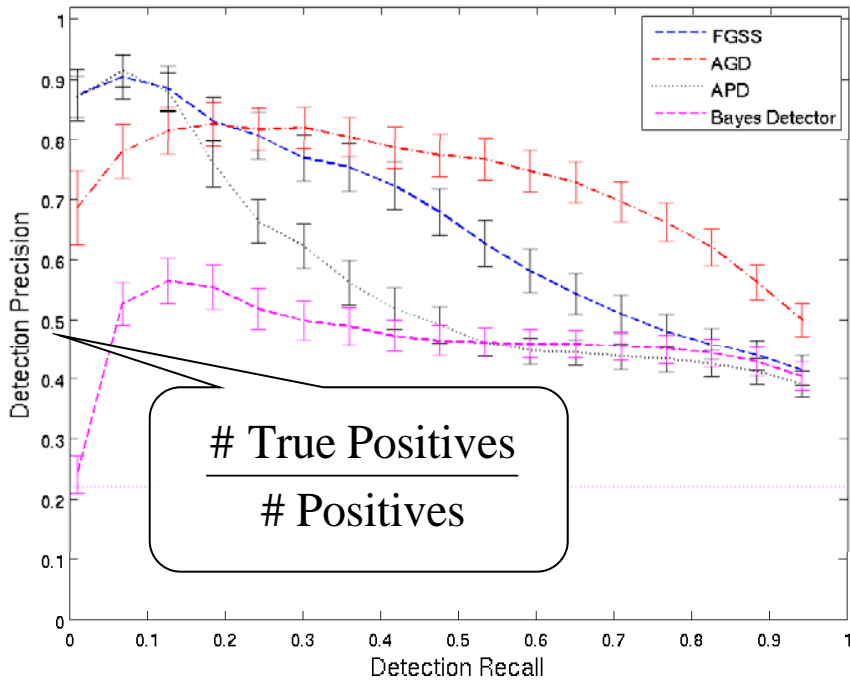
Run Times (100,000 Records)



 **Exhaustive FGSS (Constrained)**  **FGSS (Constrained)**  **AGD**

(BARD) Simulated Anthrax ED Dataset

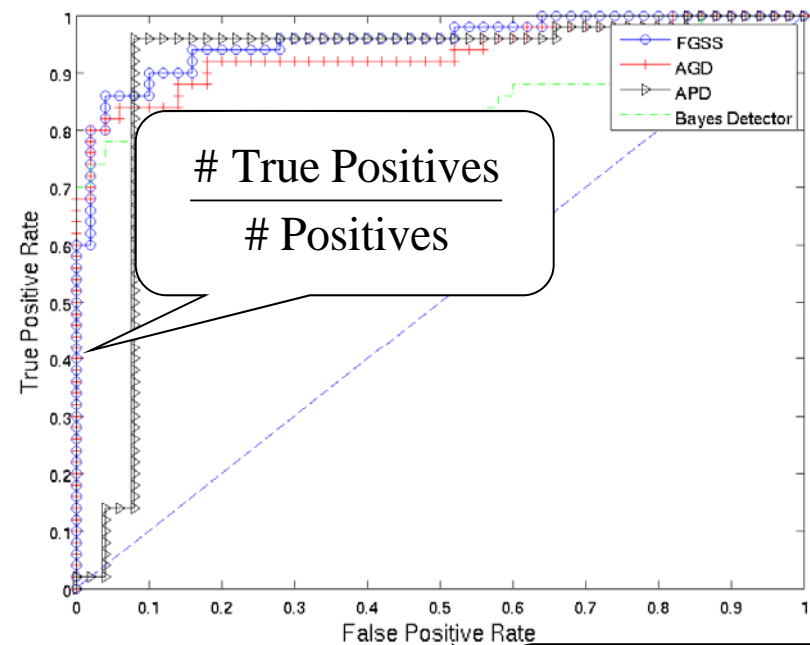
Precision vs. Recall



$$\frac{\# \text{ True Positives}}{\# \text{ Positives}}$$

The proportion of true anomalies detected.

Receiver Operator Characteristic

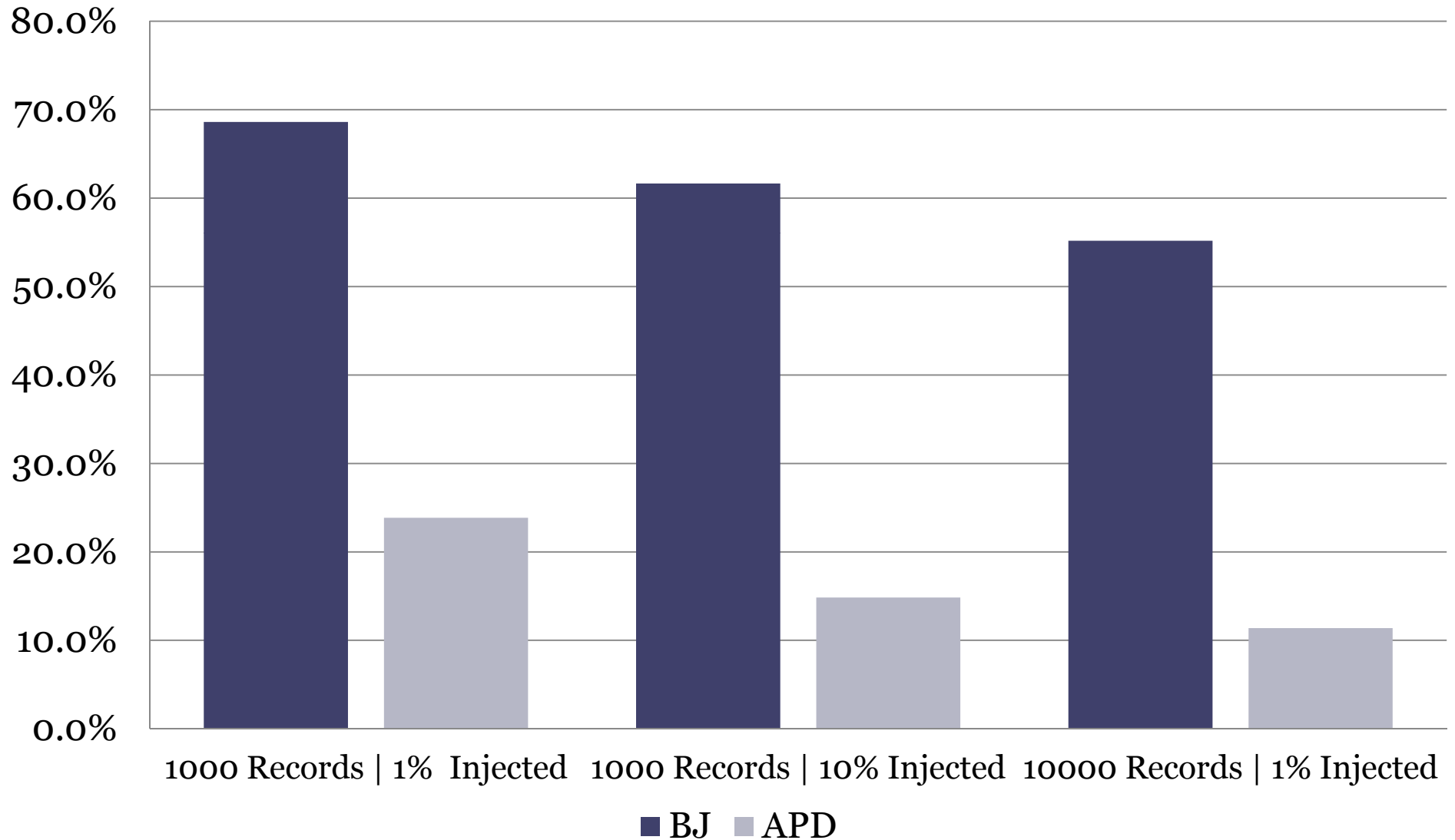


$$\frac{\# \text{ True Positives}}{\# \text{ Positives}}$$

$$\frac{\# \text{ False Positives}}{\# \text{ Positives}}$$

Results

Pattern Characterization Accuracy



Conclusions

- FGSS run significantly faster than methods with comparable detection power
- FGSS out performs other methods when patterns are:
 - a small portion of the data
 - subtle (not extremely individually anomalous)
- FGSS can characterize anomalous patterns
- Extensions
 - Extend method to handle multiple anomaly detectors
 - Extend method to handle multiple models
 - Active Learning



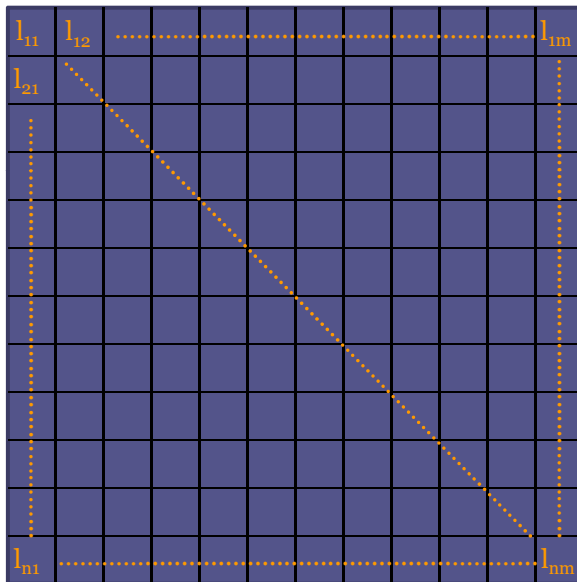
Extensions

(Preliminary)

Fast Generalized Subset Scan (FGSS)

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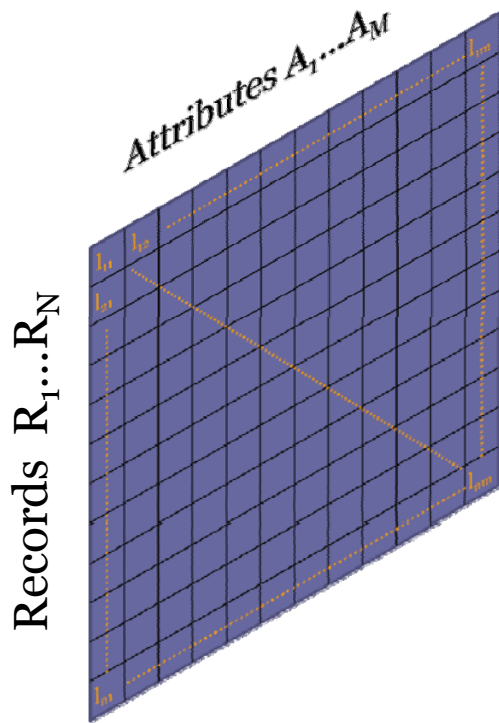
Records $R_1 \dots R_N$



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By performing inference on the Bayesian Network, for each record we can determine the likelihood of each of its attribute values

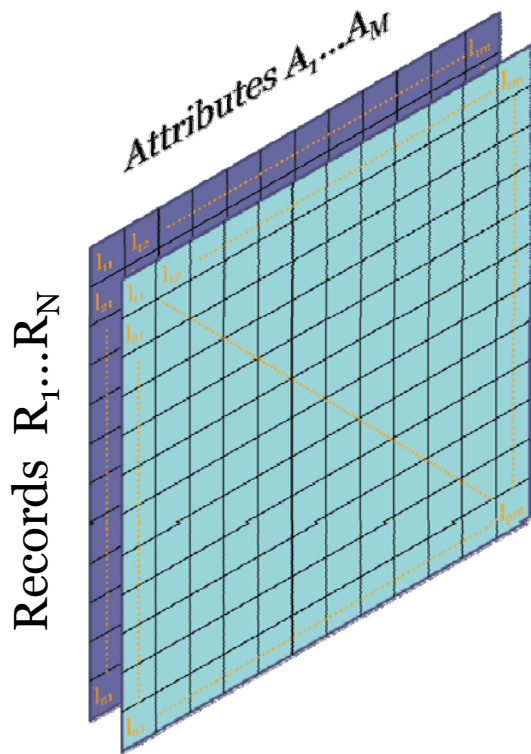
Multiple Anomaly Detectors



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 2. Compute attribute value likelihood

By performing inference on the Bayesian Network, for each record we can determine the likelihood of each of its attribute values

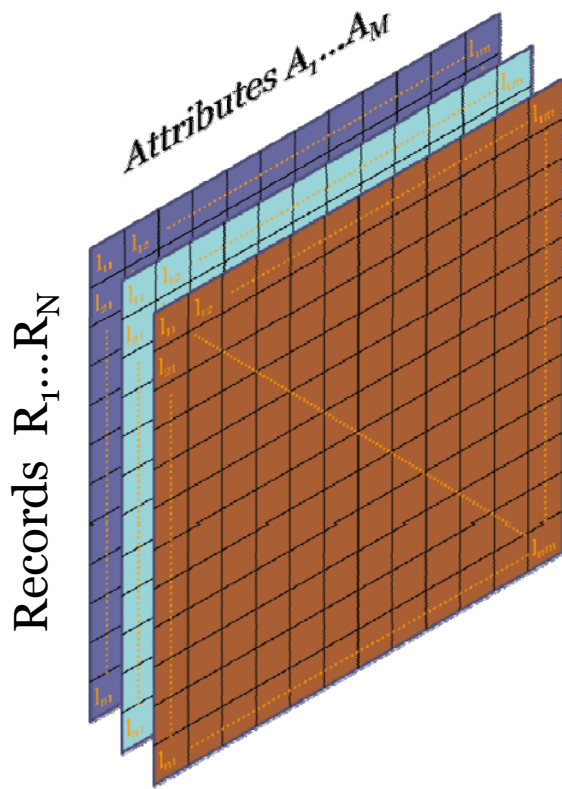
Multiple Anomaly Detectors



- I. Compute the anomalousness of each attribute (for each record)
 1. Learn Bayesian Network
 2. Compute outlier scores

Is the value sufficiently far away from the mean (outlier)?

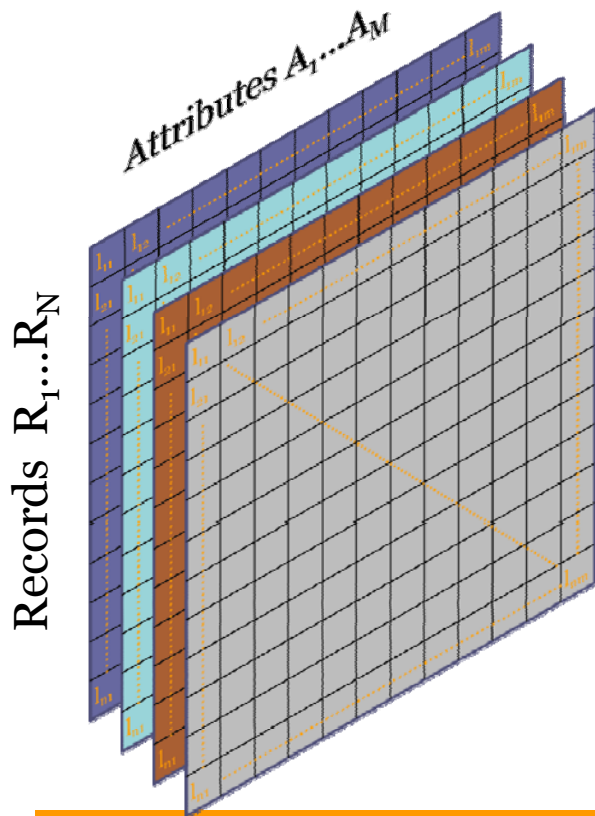
Multiple Anomaly Detectors



- I. Compute the anomalousness of each attribute (for each record)
 1. Learn Bayesian Network
 2. Compute duplicate scores

Is the value a duplicate?

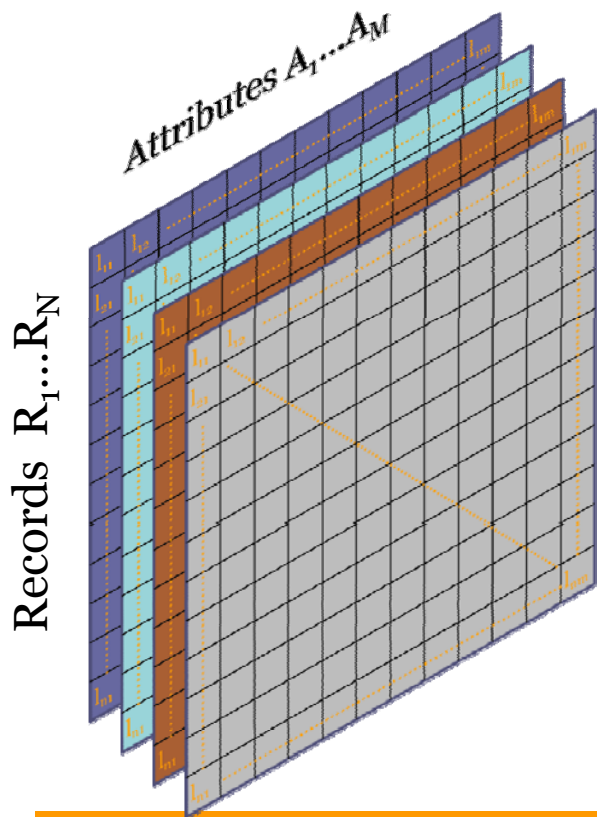
Multiple Anomaly Detectors



Is the value missing?

- I. Compute the anomalousness of each attribute (for each record)
 1. Learn Bayesian Network
 2. Compute missing scores

Multiple Anomaly Detectors



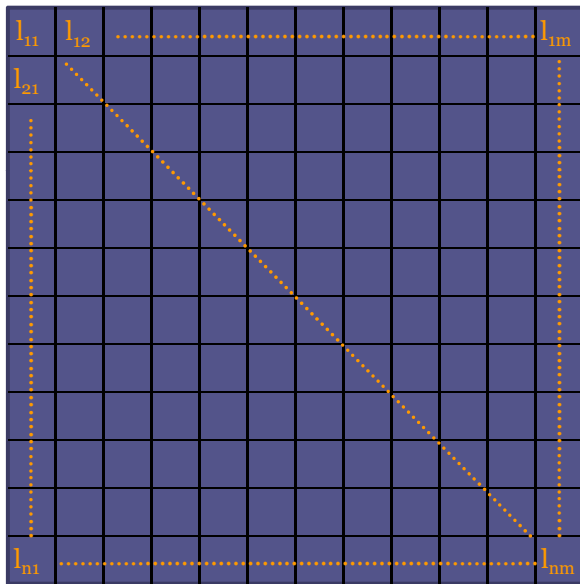
- I. Compute the anomalousness of each attribute (for each record)
 1. Learn Bayesian Network
 2. Compute anomaly scores

$$l_{ij} = \frac{\sum \alpha_k * I(isAnom(l_{ijk}))}{K}$$

Multiple Anomaly Detectors

Attributes $A_1 \dots A_M$

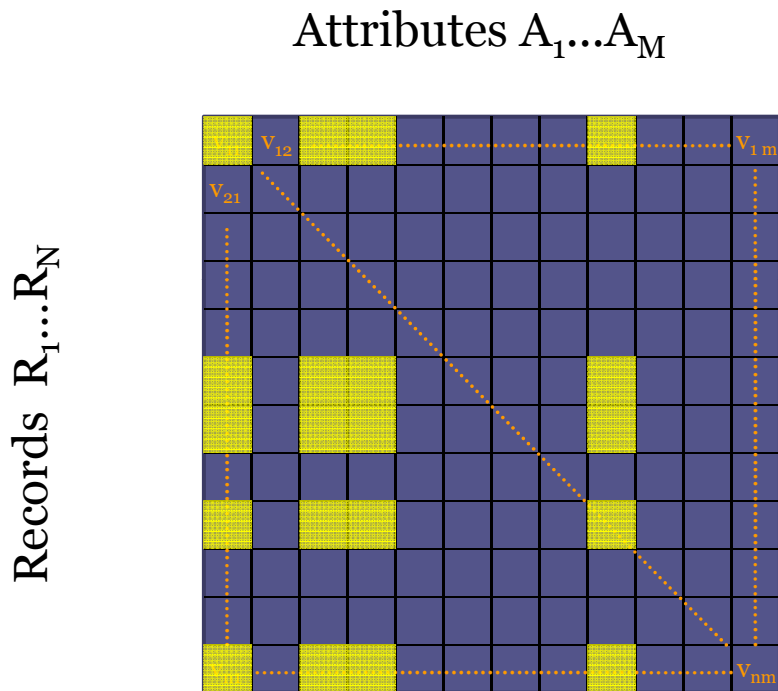
Records $R_1 \dots R_N$



- I. Compute the anomalousness of each attribute (for each record)
 1. Learn Bayesian Network
 2. Compute glitch scores

Now have new measure of the anomalous each record x attribute pair.

Multiple Anomaly Detectors



Search over all possible subsets of data and find the maximizing $F(S)$

- I. Compute the anomalousness of each attribute (for each record)
 1. Learn Bayesian Network
 2. Compute glitch scores
 3. Compute empirical p-values
- II. Discover subsets of records and attributes that are most anomalous
 1. Maximize $F(S)$ over all subsets of S
 - Iterate between following steps
 - i. LTSS over records $O(N \log N)$
 - ii. LTSS over attributes $O(M \log M)$



Thank You...Questions/Comments?