

# A Disambiguation Algorithm for Finite Automata and Functional Transducers

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Many thanks to Cyril Allauzen for the presentation!

# Motivation

- Optimization algorithms to increase efficiency of use.
- **Determinization**: substantial impact in text and speech and bioinformatics applications. But,
  - some finite-state transducers or weighted automata are not determinizable.
  - in some cases, the result is prohibitively large.
- **Disambiguation**:
  - applies to a broader set of finite-state transducers or weighted automata.
  - result can be exponentially smaller.

# Disambiguation

- **Unambiguous** automata or transducers: no two accepting paths have the same (input) label.
- **Disambiguation**: algorithm returning an unambiguous automaton or transducer equivalent to the input.

# Previous Work

- Disambiguation using determinization: standard determinization of finite automata, or transducer determinization (MM, 1997).
  - only for determinizable transducers.
- Construction of Schützenberger (1976), see also discussion by Sakarovitch (1998), and description in introductory chapter of Roche and Schabes (1997).
  - works for functional transducers.

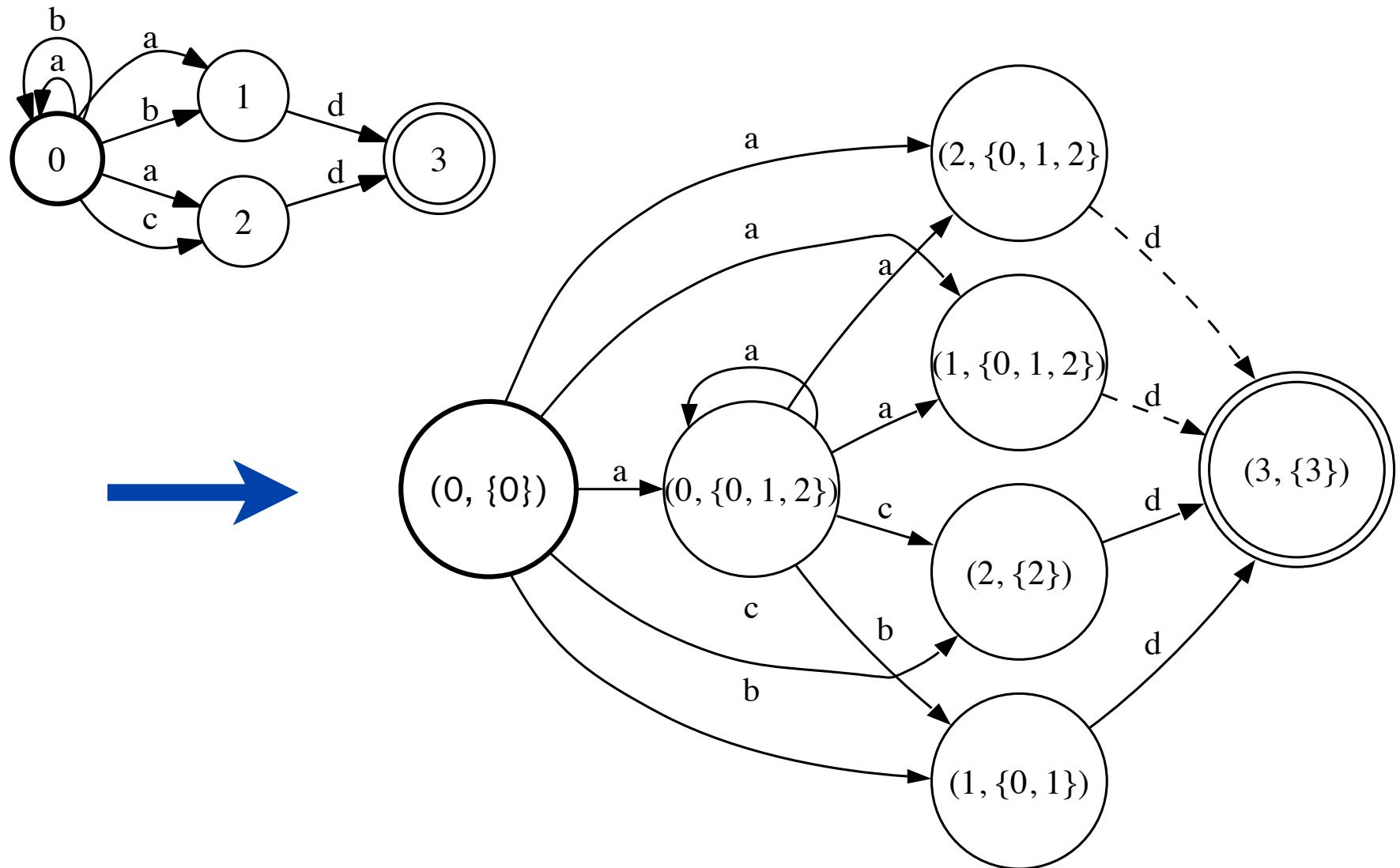
# Outline

- Schützenberger's construction.
- New disambiguation algorithm.
- Extension to automata with  $\epsilon$ -transitions.
- Disambiguation of functional transducers.

# Schützenberger's Construction

- **Overview:** transducer  $T$ , with corresponding input automaton  $A$ .
  - **compute**  $\text{det}(A)$ .
  - **compose**  $\text{det}(A) \circ T$ , with the following rule: if two states in composition  $(p, s)$  and  $(q, s)$  admit a transition with the same label to the same state, keep only one of these transitions. Idem for finality.
  -  the construction already requires determinization!

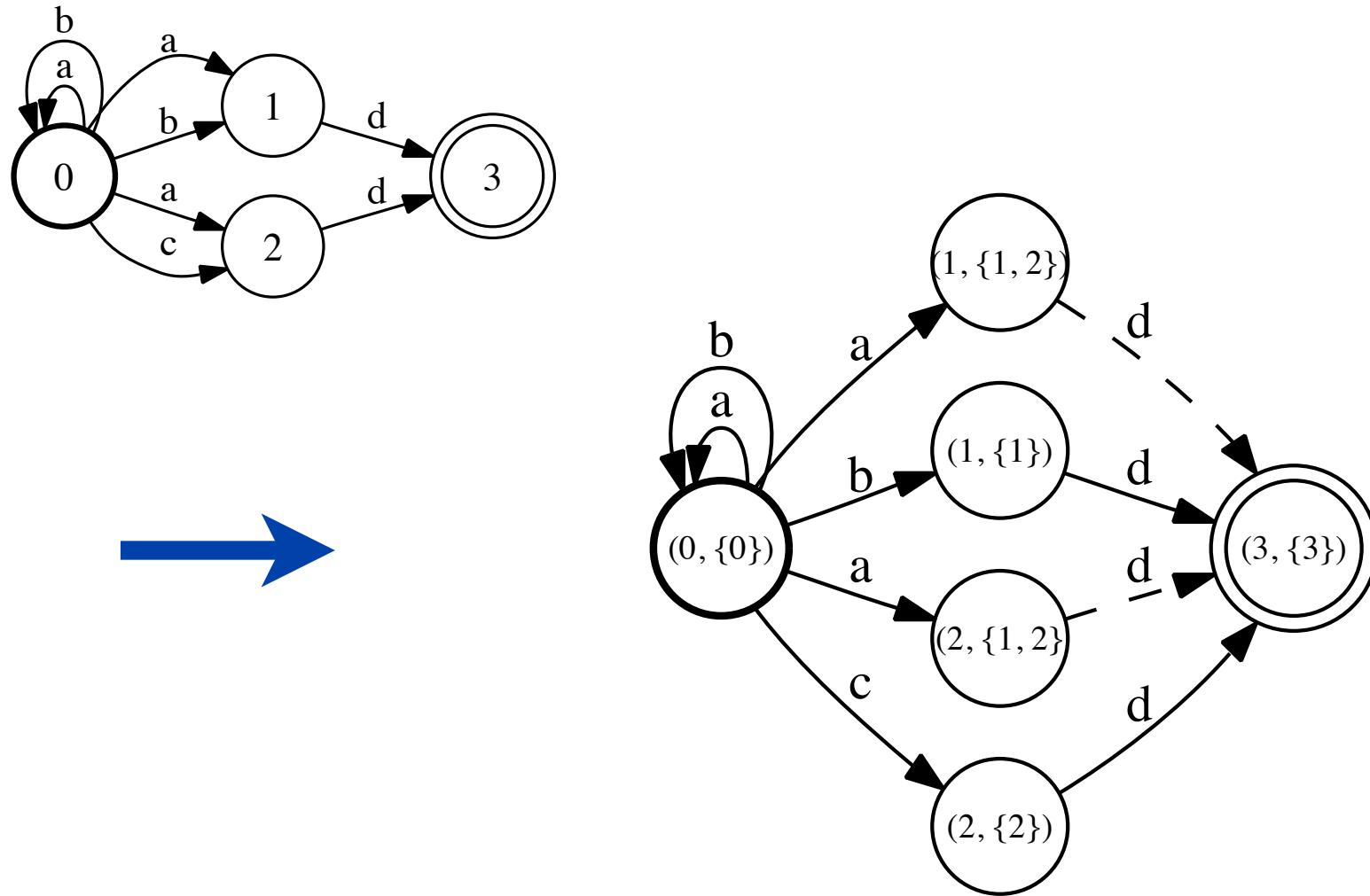
# Schütz Construction - Illustration



# New Disambiguation Algorithm

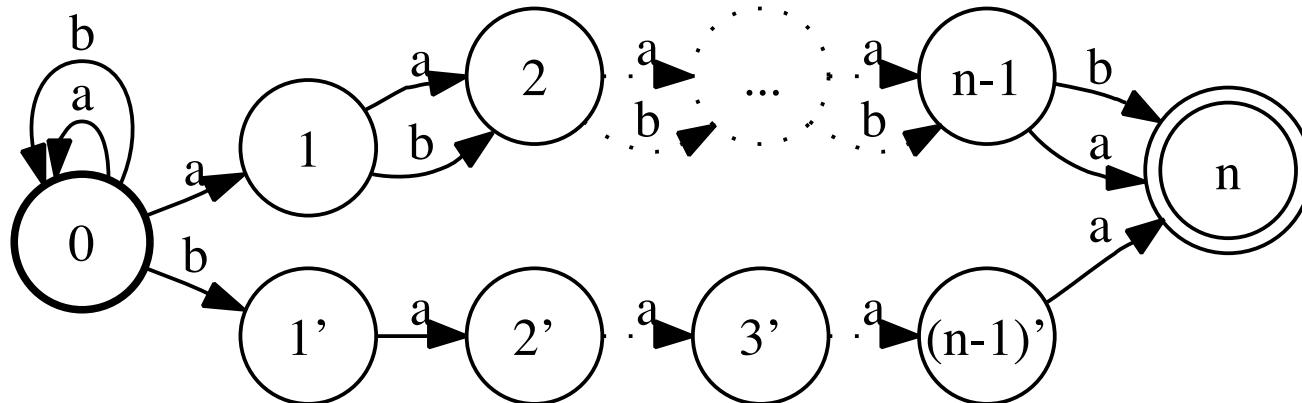
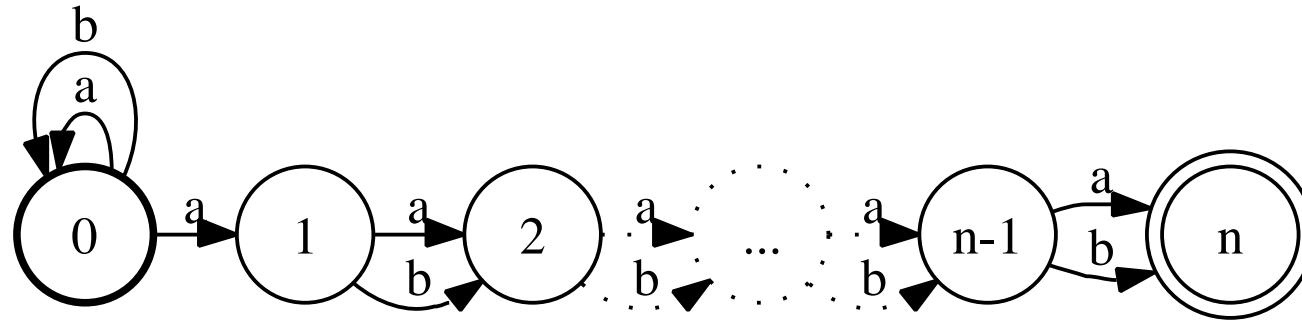
- **Key ideas:** for pair  $(p, s)$  with subset  $s$ .
  - no need to keep state  $q$  in  $s$  that does not admit a common future with  $p$ .
  - testing if  $p$  and  $q$  share common future can be done in constant time using  $B = \text{trim}(A \circ A)$ .
  -  does not require determinization.

# New Disambiguation - Illustration



# New Disambiguation - Comparison

- **Examples:** Schütz construction: exponentially larger output because of the need for determinization.  
New algorithm: same automaton or linear output.

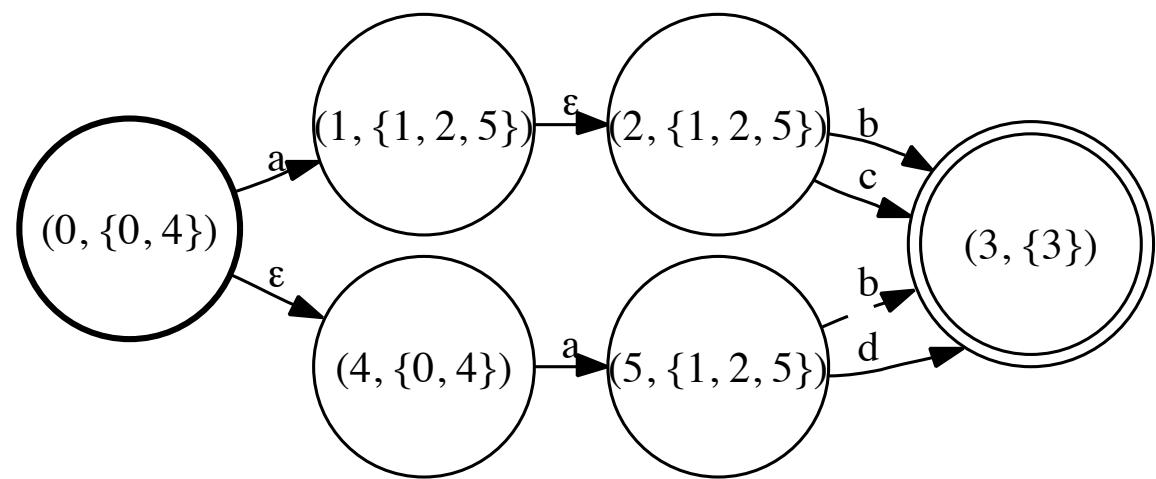
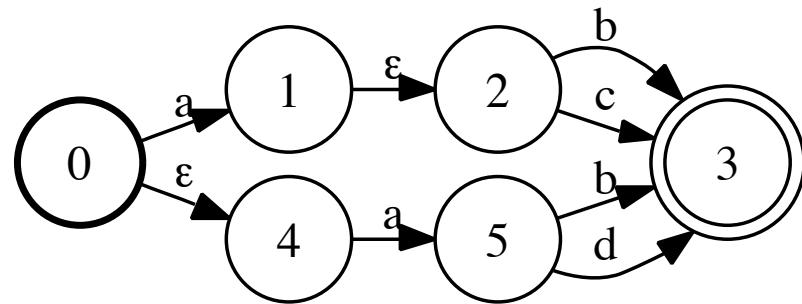


# Automata with $\epsilon$ -transitions

## ■ Extension:

- define subsets using the  $\epsilon$ -closure of the states.
- computation of  $B = \text{trim}(A \circ A)$  as in the case of automata without  $\epsilon$ -transitions.
- co-reachability of the states of output machine takes into account  $\epsilon$ -transitions.

# Automata with $\epsilon$ -transitions - Illust.



# Functional Transducers

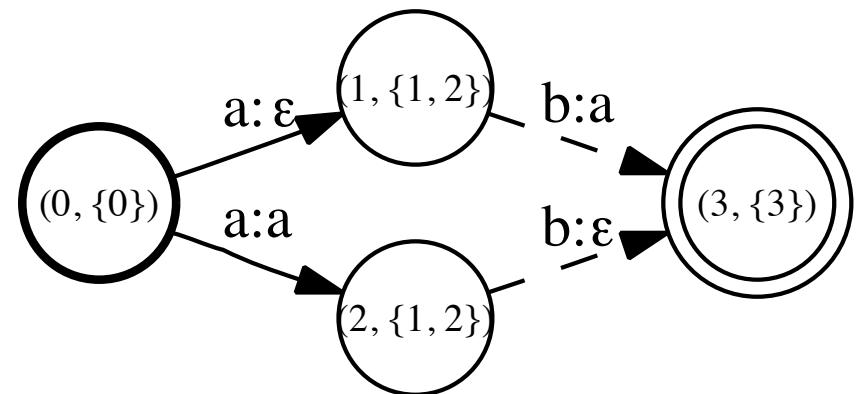
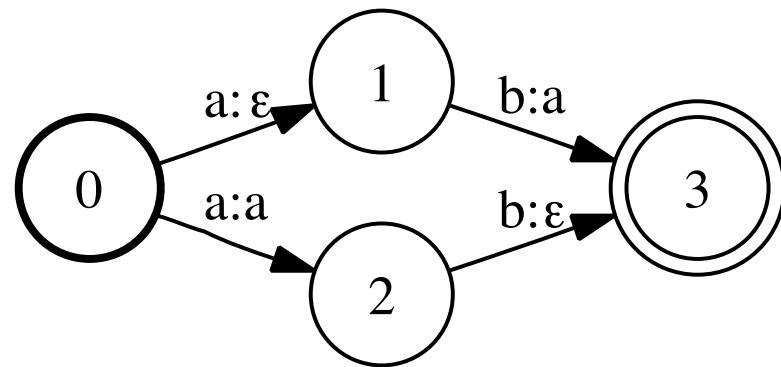
- **Functional transducers**: transducers representing partial functions. Thus, at most one output string for any input string.
- **Theorem**: functionality of transducers with output alphabet  $\Delta$  can be tested in  $O(|E|^2 + |\Delta| |Q|^2)$ , see (Allauzen and MM, 2003).

# Disamb. of Functional Transducers

## ■ Algorithm:

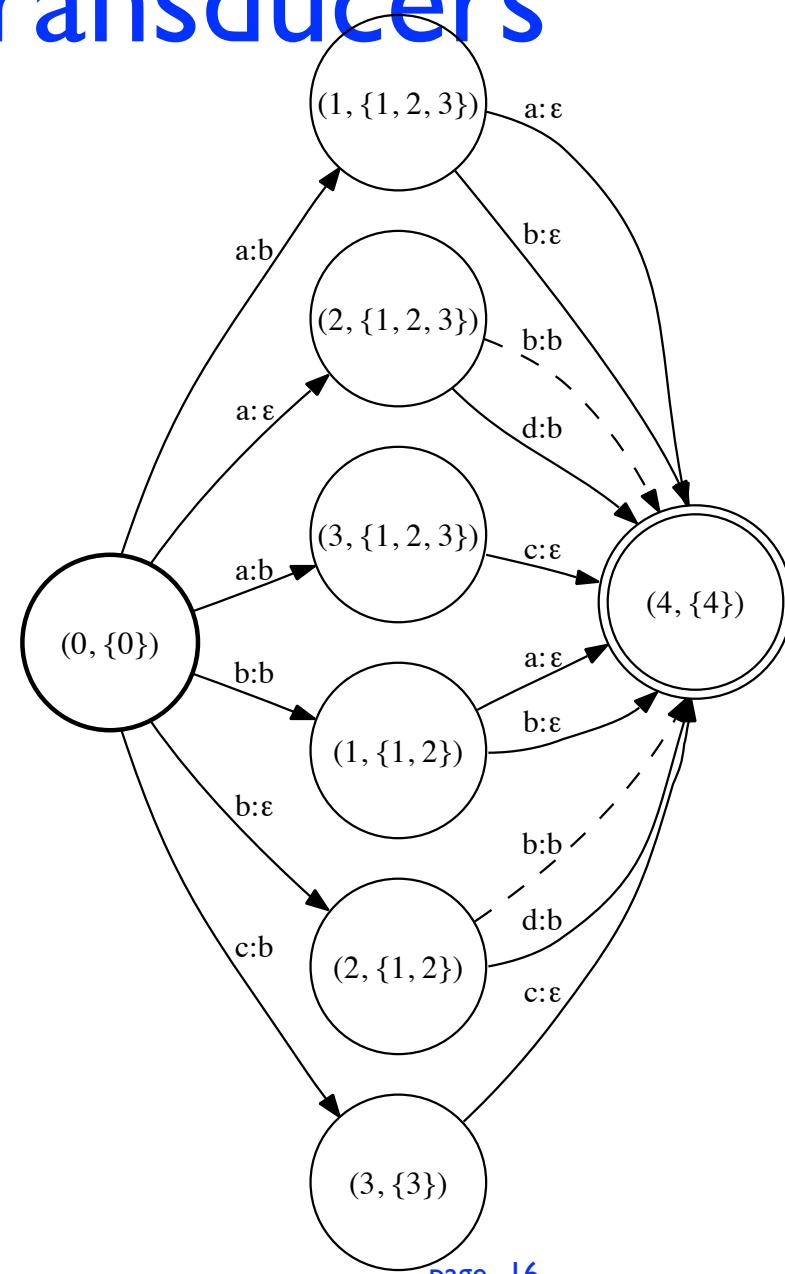
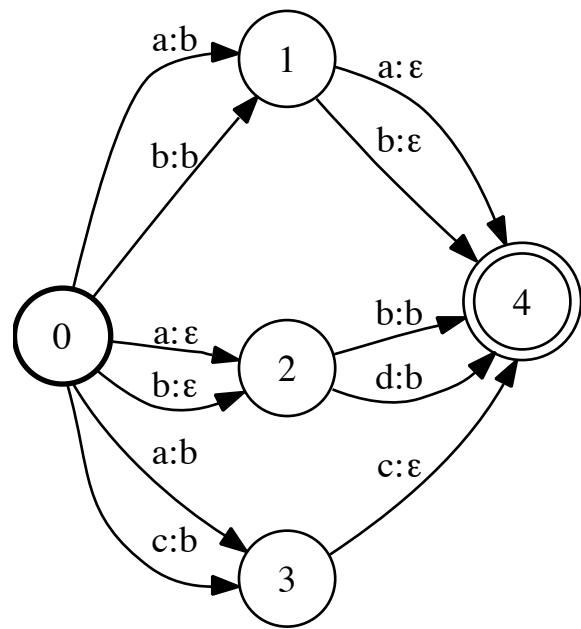
- same as for automata since only input labels matter.
- advantage over determinization: not all functional transducers are determinizable.
- advantage over Schütz's construction: output often substantially smaller, in some cases exponentially.

# Disambiguation - Illustration



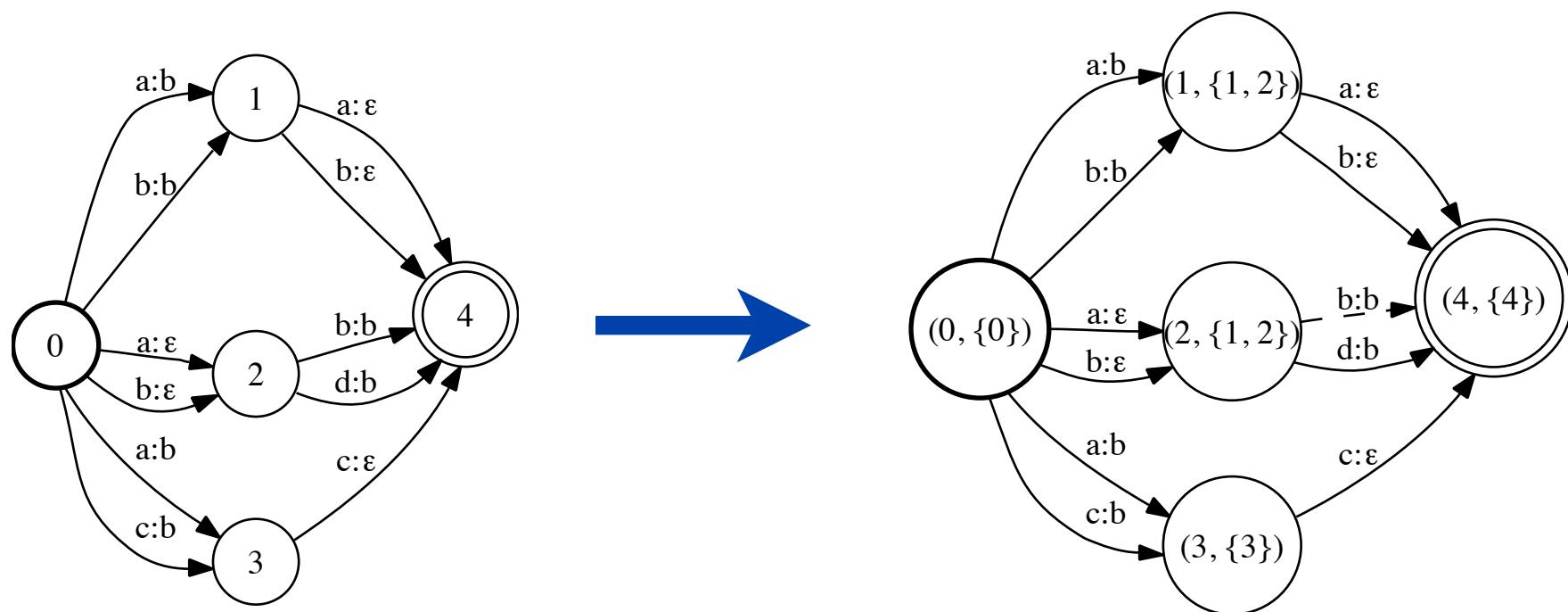
# Schütz Construction - Comparison

## Functional Transducers



# New Disambiguation - Comparison

## Functional Transducers



# Conclusion

- Disambiguation of finite automata and functional transducers.
  - optimization algorithm with wider applicability than determinization.
  - practical importance in text and speech processing and bioinformatics applications.
- Disambiguation of broad families of weighted automata and transducers.
  - extension to be presented elsewhere.
  - theoretical analysis and guarantees.