Instruction Selection by Tree Matching

- Work on AST or on DAG for basic block
- Use patterns to describe semantics of machine instructions
- Cover tree with smallest/cheapest set of patterns
- Use a greedy strategy to find good covering, or
- Use dynamic programming to find optimal covering
- Generate patterns automatically from machine description files

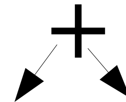
Greedy strategy: the maximal munch approach

- Construct tree patterns for each machine instruction
- Cover (tile) the AST with matching tree patterns.
- Proceed top-down, and try larger patterns first, to minimize total number of instructions.
- Traverse tree top-down and emit instructions (in reverse order)
- Algorithm is fast but does not guarantee optimality

Instructions and their pattern trees

- ADD $r_j = r_j + r_k$

+



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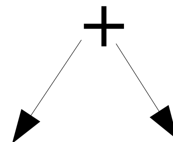
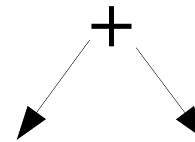
- ADDI $r_i = r_i + c$

+ + const





const const

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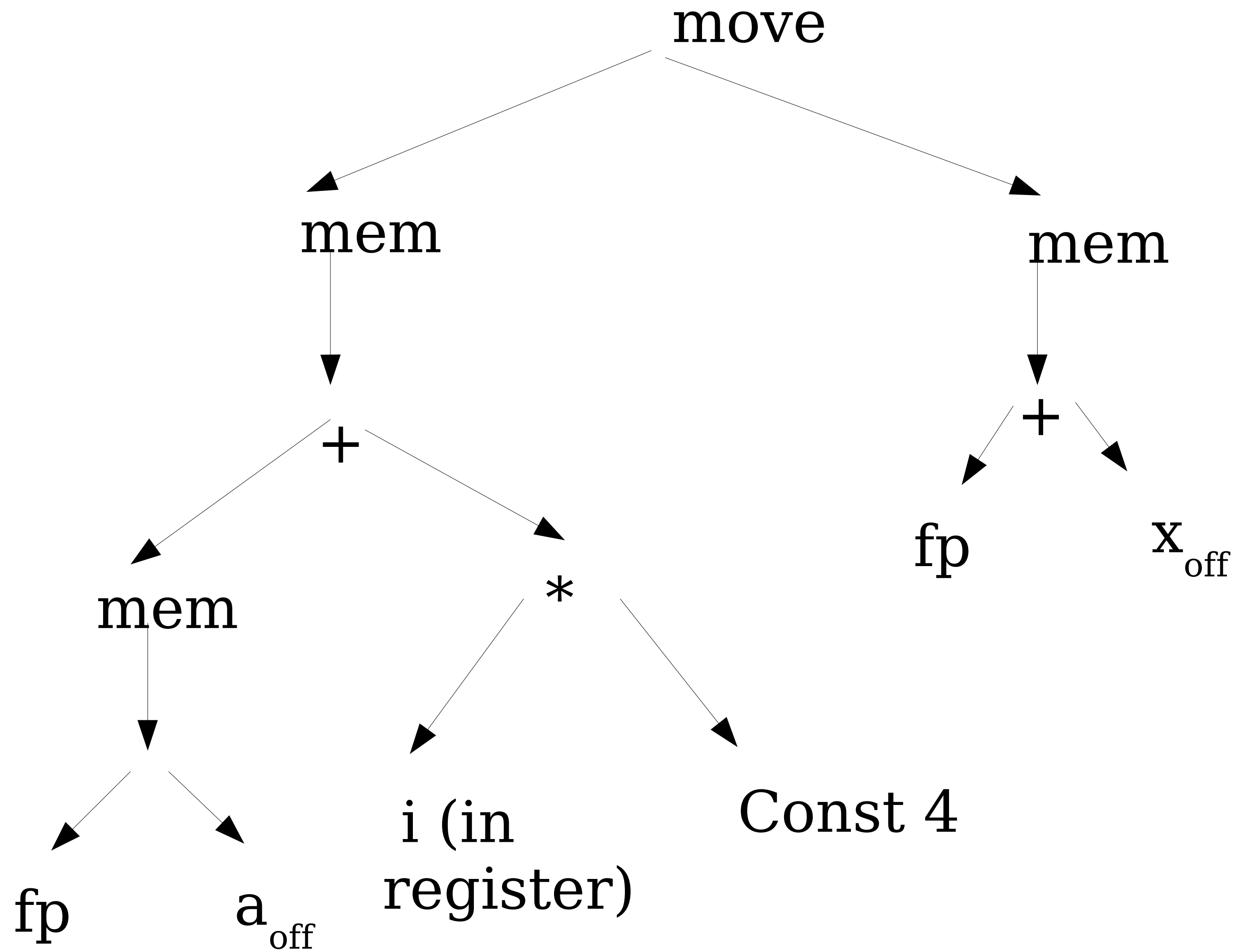
- Express commutativity, and note that an addition can effect the load of a constant
- LOAD $r_i = M[r_j + c]$ 4 trees.
- Assume frame pointer in register, and $r_0 = 0$ always.

Example: tiling for a[i] = x

- 

Naïve tiling: 10 instructions

- ADDI r1 = r0 + a // load offset of a
- ADD r1 = fp + r1 // address of a
- LOAD r1 = M[r1 + 0] // load a
- ADDI r2 = r0 + 4 // load constant 4
- MUL r2 = ri * r2 // scale i by 4
- ADD r1 = r1 + r2 // base + index
- ADDI r2 = r0 + x // load offset of x
- ADD r2 = fp + r2 // address of x
- LOAD r2 = M [r2 + 0] // load x
- STORE M [r1 + 0] = r2 // store x in array

Better tiling: 3 memory accesses 6 instructions

- LOAD $r_1 = M[fp + a]$
- ADDI $r_2 = r_0 + 4$
- MUL $r_2 = r_i * r_2$
- ADD $r_1 = r_1 + r_2$
- LOAD $r_2 = M[fp + x]$
- STORE $M[r_1 + 0] = r_2$

Best tiling: two memory instructions

- LOAD $r_1 = M[fp + a]$ // load a
- ADDI $r_2 = r_0 + 4$ // load 4
- MUL $r_2 = r_i * r_2$ // scale i
- ADD $r_1 = r_1 + r_2$ // address of a[i]
- ADDI $r_2 = fp + x$ // address of x
- MOVEM $M[r_1] = M[r_2]$ // memory copy

The maximal munch algorithm

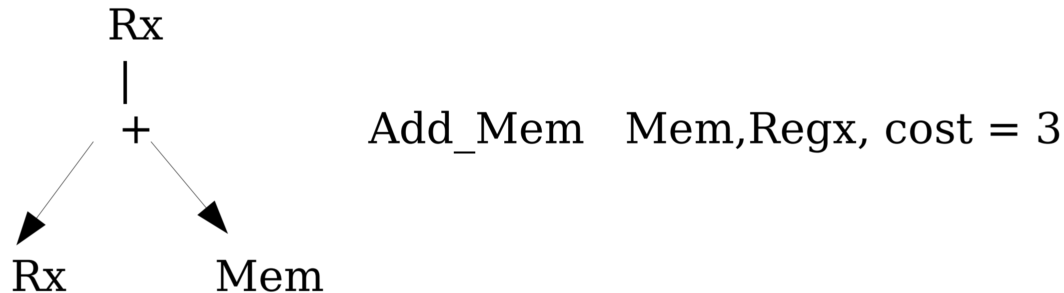
- Top-down procedure.
- Order pattern trees by size, largest first
- Tree matches if operator matches and if descendants match (recursive)
- Different procedure for statements and for expressions.

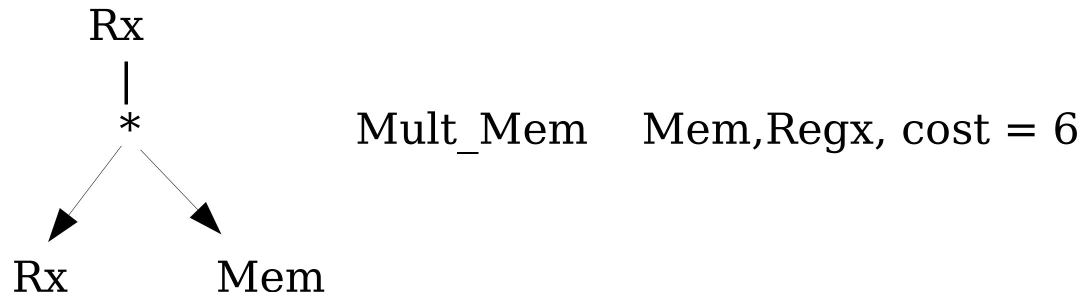
Example: matching a move subtree

- **if** (op = "+"
-     && kind (right_operand) == Constant){
-   Munch (left_operand);
-   Emit (store_instruction);
- **else if** (op = "+"
-     && kind (left_operand) == Constant) {
-   Munch (right_operand);
-   Emit (store_instruction);
- **else** ...

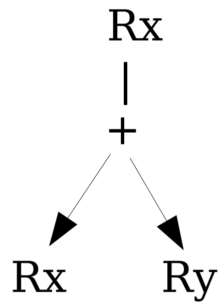
BURS
bottom-up rewriting System

- Describe machine instructions by tree patterns:

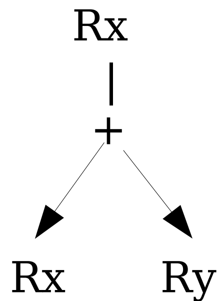




All operations have costs



Add_Reg Rx, Ry   cost = 2



Mult_Mem Mem,Regx, cost = 3

Three-pass algorithm

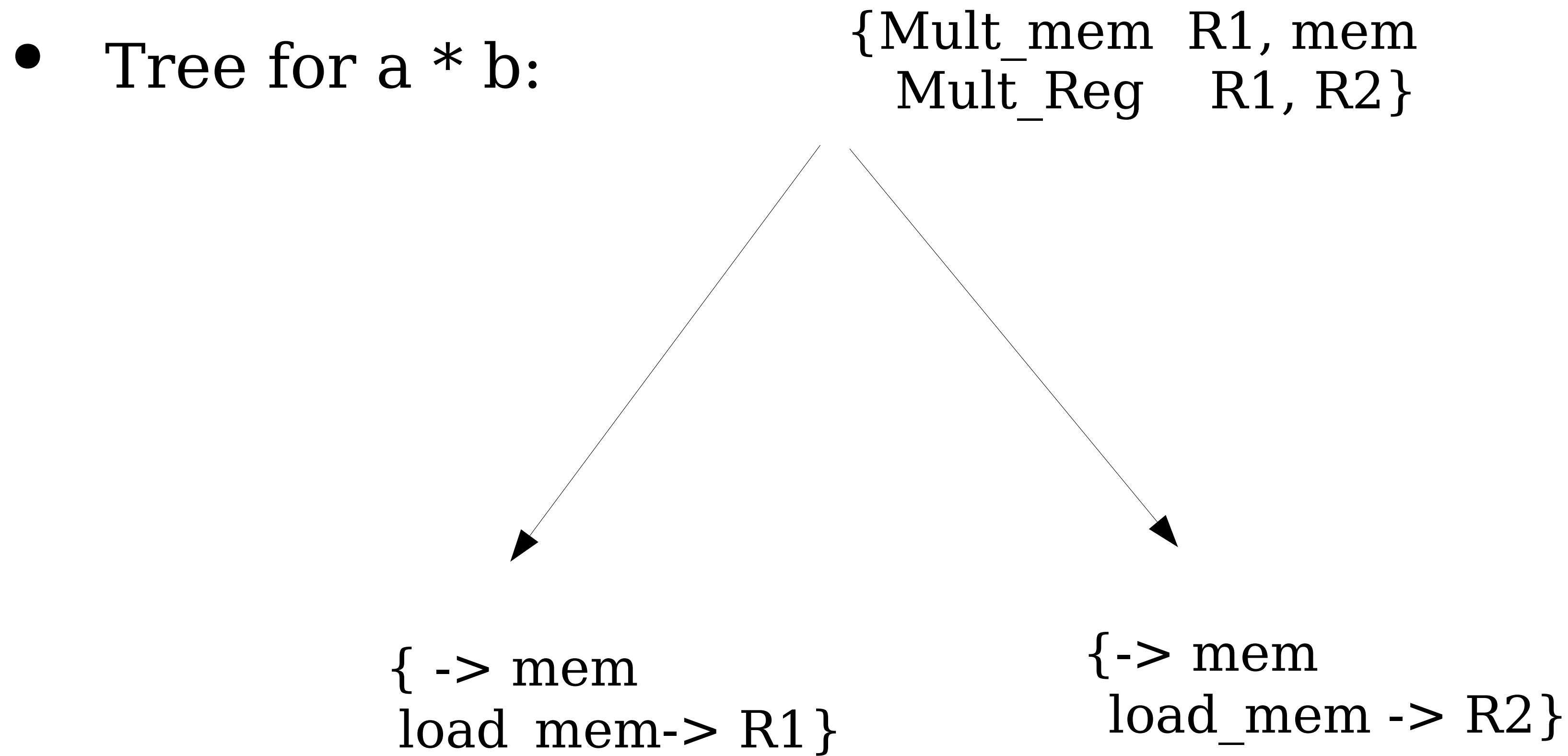
- Instruction-collecting: bottom-up tree matching, using cost information.
  - Each node has set of candidates
- Instruction selection: top-down pass to select single interpretation for node
- Code generation: bottom-up traversal to emit instructions in proper order

Tree Matching

- Similar approach to LR parsing:
  - Introduce **items**: patterns with dot, indicating partial match.
  - Label tree nodes with sets of items
  - Extend match by moving dot
  - Item with dot at root represents full match of instruction (like accept state)

Computing label sets for nodes

- Tree for a * b:



Bottom-up pattern matching

- To annotate node N with a set of possible matches (labels):
  - Match left operand
  - Match right operand
  - For each tree pattern P
    - For each label of left operand L1
      - For each label of right operand L2
      - If matches (P, L1, L2) then
        - Compute cost of (L1, L2) and add label to N
        -
- At each level, keep cheapest labelling (there maybe several of them)

Automating the process

- Describe semantics of instruction set in a machine description file
- Generate tree patterns automatically
- Generate automaton to guide pattern match
- Pattern-matching code is machine-independent, produces machine-specific code.

Example: some patterns for lcc on X86

- Describe a memory location:
  - mrc1: mem %0 1 // load, cost 1
  - mrc1: rc %0
  -
- Describe addition with one operand in memory
  - reg:ADDI (reg, mrc1) (pattern on X86)
  - ?mov %c, %0, // may need a load
  - add %c, %1 1 // cost 1

References

- Maximal munch:
  - Andrew Appel: modern compiler implementation in X (for various values of X)
- BURS:
  - Brune,Bal, et al: Modern Compiler Design
- Original paper:
  - Proebsting: TOPLAS 17 (3) AMY 1995
- LCC:
  - Fraser & Hanson: A retargetable C compiler